

1. C Only two. 1,2,3,5,6 and 1,2,3,4,7
2. D Triangle Inequality: $14L+1 > 3L+4$ $11L > 3$ $L > 3/11$
3. A Graph it and you get a right triangle in Q3 with a base of 2 and a height of 2 and unbounded region from $x \leq -2$.
4. C $3^{5k} \cdot 3^{-4k} \geq 3^{2k^2-6} \rightarrow k \geq 2k^2 - 6 \rightarrow 2k^2 - k - 6 \leq 0$
 $(2k+3)(k-2) \leq 0 \rightarrow \left[\frac{-3}{2}, 2 \right] \rightarrow 0, 1, 2$ so a total of 3
5. A $y^2 - 6y + 9 = -8x - 25 + 9 \rightarrow (y-3)^2 = -8(x+2)$
 $V = (-2, 3) \rightarrow p = -2 \rightarrow x = 0$
6. A This is a vertical hyperbola so Y-squared is positive and x-squared is negative. We are centered at the origin and $2a=4$ so $a=2$. $c = \sqrt{7}$, $a^2 = 4$, $b^2 = 3 \rightarrow \frac{y^2}{4} - \frac{x^2}{3} = 1$
7. B $f(n) = \prod_{j=3}^n \log_{j-1} j = \frac{\log 3}{\log 2} \cdot \frac{\log 4}{\log 3} \cdot \frac{\log 5}{\log 4} \cdot \dots \cdot \frac{\log n}{\log(n-1)} = \log_2 n$
 $\sum_{k=2}^{10} f(2^k) = 2 + 3 + \dots + 10 = 54$
8. B Draw an altitude for the parallelogram down from D. It has a length of 3 so the area is 48. Call the smaller base of the trapezoid B. We get:
 $48 = \frac{1}{2} \left(8 - \frac{B}{2} \right) (16 + B) \rightarrow B = 8$
9. B $M + 3R = 14$
 $M + 3L = 16$ so the average is 4
 $M + 3U = 18 \rightarrow 3(M + R + L + U) = 48 \rightarrow (M + R + L + U) = 16$
10. B $\frac{8}{k-1} - k - 1 < 0 \rightarrow \frac{8 - k^2 + 1}{k-1} < 0 \rightarrow \frac{-(k-3)(k+3)}{k-1} < 0$
 $(-3, 1) \cup (3, 5) \rightarrow \frac{6}{10} \rightarrow 60\%$
11. C $\frac{4\pi \cdot 9}{2\pi \cdot \frac{1}{4}} = 72$
12. A $\frac{R}{R+1} + \frac{2R+1}{R^2+R} = 6 \rightarrow R^2 + 2R + 1 = 6R^2 + 6R$
 $5R^2 + 4R - 1 = 0 \rightarrow R = \frac{1}{5} \rightarrow \frac{\frac{1}{5} + \frac{7}{5}}{6} = \frac{4}{15}$
13. A $(1+i)(1+i) = 2i \rightarrow (2i)^6 (1+i) = -64(1+i) \rightarrow -64 - 64 = -128$
14. E $y = \sqrt{-(x^2 - 6x + 9)} = \sqrt{-(x-3)^2}$. This is a point (3,0) so the answer is 3

15. A $-6-5-2+3=-10$
16. D The base can be 2 raised to any factor of 20. Those are 1,2,4,5,10,20 so there are 6
17. D The common difference must be a common factor of 63 and 175 since $256-81=175$ and $144-81=63$. The common factor is 7 s $25+1=26$
18. B They could both get 0,1,2, or 3 tails $\frac{1}{8} \cdot \frac{1}{8} + \frac{3}{8} \cdot \frac{3}{8} + \frac{3}{8} \cdot \frac{3}{8} + \frac{1}{8} \cdot \frac{1}{8} = \frac{20}{64} = \frac{5}{16}$
19. A Ratio of the areas is 16/9 so the ratio of the lengths is 4/3. The triangles share an altitude so the area of each is 4/3 of 18 which is 24 so $18+32+24+24=98$
20. D $(2^8 + 1)(2^4 - 1)(2^4 + 1) = 3 \cdot 5 \cdot 17 \cdot 257 \rightarrow 15, 17, 51, 85 \rightarrow 4$
21. C $\frac{\sin 45}{9} = \frac{8}{9(MA)} \rightarrow MA = 8\sqrt{2} \rightarrow (8\sqrt{2})^2 = 128 \rightarrow 1+2+8=11$. You could also draw an altitude and work it that way.
22. C Draw a good picture. LUO and LZO are 30-60-90 triangles. $LO = \frac{\sqrt{3}}{2}$. ZLA is also a 30-60-90 with $ZL = 1/2$. This makes $ZA = 1/4$ and $LA = \frac{\sqrt{3}}{4}$. The area is $\frac{1}{2} \cdot \frac{\sqrt{3}}{4} \cdot \frac{1}{4} = \frac{\sqrt{3}}{32}$
23. A $k = 2x^2 - 12x + 16 \rightarrow 2x^2 - 12x + 16 - k = 0$
 $D = 0 = 144 - 4 \cdot 2(16 - k) \rightarrow k = -2$
24. D Classic Venn diagram question. Draw your 3 circles and call x all 3. $400-164=236$. $39+51+x=236-117=119$ so $x = 29$
25. E September has 30 days. October 2 is first Monday so 5th Monday of October is 10/30
26. D $N + D + Q = 20$
 $5N + 10D + 25Q = 335$
 $N + 2D + 5Q = 67$
 $D + 4Q = 47 \rightarrow 25N + 5D + 10Q = 275 \rightarrow 5N + D + 2Q = 55$
 $9D + 23Q = 280 \rightarrow Q = 11$
27. C Draw a big picture. Call angles UFL and LUF "y". Call WUZ and ZUW both "x". If we work around the triangle we get $x+y=135$. The angle we want is $180-135$ so answer is 45
28. D Draw a segment from the center of circle X to segment QY to create a rectangle with dimensions of 20 by 5. This creates a right triangle with legs of 20 and 3. We want the hypotenuse so $\sqrt{400+9} = \sqrt{409}$
29. C Check endpoints and vertex. Complete the square to get $\sqrt{-16\left(t^2 - 3t + \frac{9}{4}\right) + 38}$ If you plug in 0 you get 2 and the vertex gives you 38 but if you plug in 4 and take the absolute value you get 62 which is the answer
30. D The diameters are 22,24, and 26. That makes the radii 11,12, and 13. We want $4\pi r^2 = 4\pi(121+144+169) = 1736\pi$

