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Note that A must be expressed as an integer.

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Olivia Rodrigo has déjà vu! She keeps doing the same processes over and over again: She first starts with an equilateral triangle with side length 1. This triangle has area  $A_0$ . She then creates a new triangle by halving the length of all the side lengths. This triangle has area  $A_1$ . She then continues this to get  $A_2, A_3$  and so on to infinity. Let  $A = A_0 + A_1 + A_2 + A_3 + \ldots$ , or the infinite sum of all the areas of the triangles.

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Sabrina Carpenter is getting a Taste of the fundamentals of Calculus. Consider the following function f given by the table:

x	f(x)	f'(x)
-1	0	-1
0	-1	-2
1	-2	-3

Assume that  $f^{-1}$  exists and is continuous on [-1, 1]. Let A be the approximation of  $f^{-1}(1)$  using the value of  $\int_{-1}^{1} (f^{-1})'(x) dx$ , approximated by a left Riemann sum with 2 sub-intervals of length 1.

# Question #4 – Calculus Seat – 2025 MAO Nationals Convention Relay

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Billie Eilish wants to be THE GREATEST at calculus. Help her with the following problem: Let  $A = V/\pi$ , where V is the volume of the solid obtained from rotating the function  $f(x) = 2xe^{-x+1}$  on the domain  $[1, \infty)$  around the x-axis. Note that A is not the value of the volume.

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$$\pi \ln(k) = \int_0^\pi \frac{x|\cos(x)|}{1+\sin(x)} \, dx$$

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In order to test her true Solar Power, Lorde is studying orbits and considers the following (possibly degenate) conic:

$$3Ax^2 + xy + 2Ay^2 - 3Ax + 2y - 5A = 0$$

The conic is then rotated counterclockise by an acute angle  $\theta$  so that the conic no longer has an xy term. Given that  $\cos(4\theta) = 3/5$ , and that A is positive, find A.

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