

$$1. \text{ C. } m = -\left(-\frac{3}{7}\right) = \frac{3}{7}, \perp m = -\frac{7}{3}, 7x + 3y = -15, A + B + C = 25$$

$$2. \text{ C. } \sin^2 \alpha - \sin^2 \beta = \frac{(\sqrt{2} + \sqrt{6})(\sqrt{2} - \sqrt{6})}{16} = -\frac{1}{4}; \quad -\frac{1}{4} = \sin^2 \alpha - \frac{3}{4}$$

$$\pm \frac{\sqrt{2}}{2} = \sin \alpha \quad \alpha = \frac{\pi}{4} \quad \alpha \neq -\frac{\pi}{4}; \sin\left(-\frac{\pi}{4} + \frac{\pi}{3}\right) \neq \frac{\sqrt{2} + \sqrt{6}}{4}$$

$$3. \text{ B. } \begin{vmatrix} 3 & -1 & -3 & -6 & 8 \\ 2 & 5 & 2 & 1 & -4 \end{vmatrix} \quad 15 - 2 - 3 + 24 + 2 + 15 + 12 - 8 = 55$$

$$A = \frac{1}{2}(55) = 27.5$$

4. D.

$$5. \text{ C. Pt. of intersection } \left(\frac{14}{11}, -\frac{6}{11}\right); \quad \left| \frac{4\left(\frac{14}{11}\right) - 5\left(-\frac{6}{11}\right) + 3}{\sqrt{41}} \right| = 1.7$$

$$6. \text{ D. } R = \frac{a}{2 \sin A}; \quad D = 2\left(\frac{12}{2 \sin 37^\circ}\right) = 19.9$$

$$7. \text{ C. } \tan \theta = \frac{\left(-\frac{7}{8}\right) - \left(\frac{4}{3}\right)}{(1) + \left(-\frac{7}{8}\right)\left(\frac{4}{3}\right)} = 13.25; \quad \tan^{-1}(\theta) = 13.25; \quad \theta = 85.7^\circ$$

8. C.

$$9. \text{ A. } \sin 4\alpha = \frac{\sqrt{3}}{2}; \quad 4\alpha = \frac{2\pi}{3}; \quad \alpha = \frac{\pi}{6}; \quad \cos 4\alpha = -\frac{1}{2}; \quad \alpha = \frac{\pi}{6}$$

$$10. \text{ C. } b + c = 12 \left( \frac{\cos\left(\frac{(63-37)}{2}\right)}{\sin\left(\frac{80}{2}\right)} \right) = 18.2; \text{ Law of Sines could also be used.}$$

$$11. \text{ A. } s = \frac{1}{2}(a + b + c) = 13; \quad r = \sqrt{\frac{(s-a)(s-b)(s-c)}{s}} = 1.6$$

$$12. \text{ C. } 2 \cosh^2 u - 1 = \frac{1 + \tanh^2 u}{1 - \tanh^2 u}; \quad 161(1 - \tanh^2 u) = 1 + \tanh^2 u;$$

$$161 - 161(\tanh^2 u) = 1 + \tanh^2 u; \quad 160 = 162 \tanh^2 u; \quad 0.99 = \tanh^2 u$$

$$13. \text{ C. } \frac{13}{\sin 67^\circ} = \frac{12}{\sin \theta}; \quad \theta = 58.2^\circ$$

$$14. \text{ C. } \frac{1 - \cos^2(\alpha)}{\sec(\alpha) \csc(\beta)} = \sin^2(\alpha) \cos(\alpha) \sin(\beta)$$

$$15. \text{ C. } n^2 = 2 + \sqrt{1+n}; \quad n^2 - 2 = \sqrt{1+n}; \quad n^4 - 4n^2 + 4 = 1+n; \quad n^4 - 4n^2 + 4 = 1+n; \quad n^4 - 4n^2 - n + 3 = 0$$

$$16. \text{ C. } a^2 = 13^2 + 5^2 - 2(13)(5)\cos(86^\circ); \quad a = 13.6$$

$$17. \text{ B. } s = 20; r = 2\sqrt{2}; \quad \tan\left(\frac{A}{2}\right) = \frac{r}{s-a} = \frac{2\sqrt{2}}{8} = \frac{\sqrt{2}}{4}$$

$$18. \text{ B. } \frac{2(\cosh^2(u) - \sinh^2(u)) \tanh(u) \cosh(u) \coth(u) \sinh(u) \csc h(u)}{\csc h(u) \tanh(u) \coth(u)} = 2 \cosh(u) \sinh(u)$$

$$2 \cosh(u) \sinh(u) = \sinh(2u)$$

$$19. \text{ D. } A = \frac{(18)(\sqrt{194})\sin(62^\circ)}{2} = 110.7$$

20. B.

$$21. \text{ D. } A = \frac{1}{2}(9)(15)(\sin 30^\circ) = 33.8$$

$$22. \text{ C. } r = 2; \tan^{-1}\left(\frac{1}{\sqrt{3}}\right) = 30^\circ; (2\text{cis}30^\circ)^{10} = 2^{10}[\cos 300^\circ + i \sin 300^\circ] = 1024\left(\frac{1}{2} - \frac{\sqrt{3}}{2}i\right) = 512(1 - i\sqrt{3})$$

$$23. \text{ B. } x = r \cos \theta; y = r \sin \theta; r - 4r \cos \theta = 2; \pm \sqrt{x^2 + y^2} - 4x = 2; x^2 + y^2 = (2 + 4x)^2; x^2 + y^2 = 4 + 16x + 16x^2; 15x^2 - y^2 + 16x + 4 = 0$$

$$24. \text{ B. } hm^2 + (a-b)m - h = 0; \theta = \tan^{-1}(m); 4m^2 + 0 - 4 = 0; m = \pm 1; -1 \text{ extraneous}; \tan^{-1}(1) = 45^\circ$$

$$25. \text{ A. } d = \sqrt{3^2 + 9^2 - 2(3)(9)\cos(354^\circ)} = 6.0$$

26. D.

$$\vec{F}_R = 50\hat{i} - 40\hat{j} + 180\hat{k}; |\vec{F}_R| = 191.05; \vec{u}_{F_R} = \frac{\vec{F}_R}{|\vec{F}_R|} = 0.262\hat{i} - 0.209\hat{j} + 0.942\hat{k}$$

$$\cos \alpha = 0.262; \cos \beta = -0.209; \cos \gamma = 0.942; \alpha = 74.8^\circ; \beta = 102.1^\circ; \gamma = 19.6^\circ;$$

$$74.8^\circ + 102.1^\circ + 19.6^\circ = 196.5^\circ$$

$$\text{Let } \vec{u}_1 = (k, 0, 0); \vec{u}_2 = (0, k, 0); \vec{u}_3 = (0, 0, k); \text{diagonal } \vec{d} = (k, k, k);$$

$$27. \text{ A. } \cos \theta = \frac{\vec{u}_1 \cdot \vec{d}}{\|\vec{u}_1\| \|\vec{d}\|} = \frac{k^2}{(k)(\sqrt{3k^2})} = \frac{1}{\sqrt{3}} \quad \theta = \cos^{-1}\left(\frac{1}{\sqrt{3}}\right) = 54.7^\circ$$

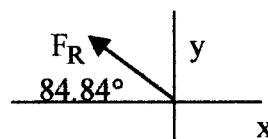
$$28. \text{ D. } \vec{u} \times (\vec{v} \times \vec{w}) = (\vec{u} \cdot \vec{w})\vec{v} - (\vec{u} \cdot \vec{v})\vec{w}; (6\hat{i} + 18\hat{j} + 24\hat{k}) - (\hat{i} - 9\hat{j} + 18\hat{k}) = 5\hat{i} + 27\hat{j} + 6\hat{k}$$

29. B.

Force	X-Component	Y-Component
F <sub>1</sub>	0	-150
F <sub>2</sub>	115.91	-31.06
F <sub>3</sub>	180	240
F <sub>4</sub>	-120	207.84
F <sub>5</sub>	-200	0
F <sub>R</sub>	-24.09	266.78

$$|\vec{F}_R| = 267.87; \theta = \tan^{-1}\left(\frac{266.78}{24.09}\right) = 84.84^\circ;$$

lies in 2<sup>nd</sup> Quadrant = 95.16



$$30. \text{ A. } V = |\vec{u} \cdot (\vec{v} \times \vec{w})|; (\vec{v} \times \vec{w}) = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} & \hat{i} & \hat{j} \\ 0 & 4 & -2 & 0 & 4 \\ 2 & 2 & -4 & 2 & 2 \end{vmatrix} = -12\hat{i} - 4\hat{j} - 8\hat{k}$$

$$|(2\hat{i} - 6\hat{j} + 2\hat{k}) \cdot (-12\hat{i} - 4\hat{j} - 8\hat{k})| = 16$$