

## Inner School Test Part B: Answers &amp; Selected solutions

1.  $44 + \frac{44}{4}$  or  $\sqrt{4}(4+4) - \frac{4}{4}$

2. -1, 1, 3

3.  $\log_{10} \frac{1}{2}$  is negative so the inequality sign (>) should have been reversed

4. 112.5 m

$$\frac{225 \text{ km}}{h} \left( \frac{1h}{60 \text{ min}} \right) \left( \frac{1000m}{1 \text{ km}} \right) \left( \frac{1 \text{ min}}{60 \text{ sec}} \right) = 62.5 \text{ m/s}$$

for 6 s  $\Rightarrow$  375m

$$\text{so } \frac{30}{100} = \frac{x}{375}$$

5.  $f(x) = \begin{cases} 2-2x; & x < 0 \\ 2; & 0 \leq x \leq 2 \\ 2x-2; & x > 2 \end{cases}$  Determine over the intervals when the values are positives

and negatives.

6. since 4, 6, 8 the LCM = 24 which implies  $24n - 1$

7. Answer: T = 10 years Therefore  $T/4 = \text{Maxima}$  and  $(3T)/4 = \text{Minima}$   
 $3(10)/4 = 7.5$  years

8. t = 25

$$y = ax^2 + bx + c$$

$$0 = a(2)^2 - 4a(2) + c$$

$$0 = 4a - 8a + c$$

$$4a = c$$

$$y = ax^2 - 4ax + 4a$$

$$1 = a(3)^2 - 4a(3) + 4a$$

$$1 = 9a - 12a + 4a$$

$$1 = a$$

Therefore,

$$c = 4(1) = 4$$

$$b = -4(1) = -4$$

$$y = x^2 - 4x + 4 \quad t = 9 - 4(-3) + 4 \quad t = 9 + 12 + 4$$

9. a) x = 78

b)  $3^{20} - 3 = x$

NOTE: All logs in this answer are in base 3.

$$40 = 20 + 5 \log(x+3)$$

$$120 = 20 - 5 \log(x+3)$$

$$\begin{array}{ll} 20 = 5 \log (x+3) & 100 = 5 \log (x+3) \\ 4 = \log (x+3) & 20 + \log (x+3) \\ & 3^{20} = x+3 \\ X + 3 = 3^4 = 81 \end{array}$$

10.  $1/2$ 

TRICKY -> For those people who went through the problem to answer the question, what is the probability of getting eleven heads in a row with a fair coin?

11. 4 coins totaling 60 cents are two nickels and two quarters

$$n = \# \text{ of coins in her purse. } \quad 15n + 10 = 14(n+1) \quad n=4$$

12.  $d = 10\text{cm}$ 

$$\begin{array}{ll} \text{Volume of } 1/2 \text{ the tank} & = 100\text{cm} * 40\text{cm} * 60\text{cm} = 240000\text{cm}^3 \\ 1/4 (240000) = 60000\text{cm}^3 & d * 100\text{cm} * 60\text{cm} = 60000 \end{array}$$

13.  $\{0, 2, -2, 3, -3\}$  Since  $x^0 = 1$  set exponent = 0 and factor.14. 5 & 97  $u = 4x^2 - 3 \Rightarrow = 4(\sqrt{2})^2 - 3 = 5$  do the same for 515.  $(x-1)^2(x+1)(x+6)(x^2+1)$  use synthetic division16.  $y = \frac{a}{b}$ , where  $b \neq 0$  Take limit as  $x$  approaches infinity

$$\begin{array}{ll} 17. (-0.423, 1.577) & \text{Set } f'(x) = 0 \\ & 4(3x^2 - 6x + 2) = 0 \\ & x = \frac{6 \pm \sqrt{12}}{6} \end{array}$$

18. 55 mph

19. 4

20.  $a = 1$   $b = 1$ 

21. 41

22.  $[2, 1, 1, 2]$ 

23. \$ 334.24

24. 1.22

25.  $b^y = a^{xy} = a$  so  $x = \frac{1}{y}$

26. Intersect in a line

27. 84 ft

28. 1025  $a_n = 2^n + 1$

29. 41 cents

30. 9