Theta Equations & Inequalities

NOTA = None of these answers

- 1. Solve for y: 4y(2 + b) b(3y 1) = 5b
- A) $\frac{4b}{8+b}$ B) $\frac{1}{2}$ C) $\frac{6b}{8+b}$ D) $\frac{6}{5}$ E) NOTA
- 2. Give the value of the discriminant for $x^2 + 3x = 10$
- A) 5 B) -5 C) 49 D) 7 E) NOTA
- 3. Determine the solution set of |2 3x| < 4.
- A) $(\frac{-2}{3},\infty)$ B) $(-\infty,\frac{-2}{3})$ C) $(\frac{-2}{3},2)$ D) $(-\infty,\frac{-2}{3})\cup(2,\infty)$ E) NOTA
- 4. A painting is twice as long as it is wide and it is held in a frame which has a uniform width of 2 inches. Find the length (in inches) of the picture, if the area of the frame is 86 square inches.
- A) $10\frac{1}{3}$ in. B) $15\frac{1}{3}$ in. C) 5 in. D) 8 in. E) NOTA
- 5. Determine the sum, x + y, of the solution of the following system of equations: 3x + y = 10x - 3y - 10 = 0
- A) 1 B) 2 C) -2 D) 0 E) NOTA
- 6. If your grade was 90 and is now 75, find the percent of decrease.
- A) $16\frac{2}{3}\%$ B) 18% C) 20% D) 22% E) NOTA
- 7. 40% of 10 inches is how many sixths of 2 feet?
- A) $\frac{1}{3}$ B) 1 C) 2 D) 4 E) NOTA
- 8. If it takes 6 hours for 4 people to paint a room, how many hours will it take 5 people, working at the same rate, to paint a room that is the same size?
- A) $3\frac{1}{3}$ B) $4\frac{4}{5}$ C) 5 D) $5\frac{1}{3}$ E) NOTA
- 9. If $a^3 = 7$, then what is the value of $4a^6$?
- A) 28 B) 56 C) 196 D) 1372 E) NOTA

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10. Find the solution(s) to the following equation: $2x + 3 + \sqrt{29 - 4x} = 0$

A) 1 B) -5 C) -4 D) -5, 1 E) NOTA

- 11. If f(x) is a polynomial function and f(2) = f(3), which of the following statements must be true?
- A) There are no real zeros between 2 and 3.
- B) There is at least one real zero between 2 and 3.
- C) 2.5 is a zero of f(x).
- D) There may be a real zero between 2 and 3.
- E) NOTA
- 12. The complex number 1 + i is a root of $2x^4 x^3 4x^2 + 10x 4 = 0$. Which of the following statements is true?
- A) There are three remaining real roots of the equation.
- B) Knowing one root of this equation is not sufficient information to find the other roots.
- C) The equation has no rational roots.
- D) There are two rational and two imaginary roots.
- E) NOTA
- 13. In calculus, one often needs to simplify an expression of the form $\frac{f(x+h)-f(x)}{h}$.

If $f(x) = \frac{1}{x+1}$ then $\frac{f(x+h) - f(x)}{h}$ simplifies to which one of the following:

A)
$$\frac{1}{h(h+1)}$$
 B) $\frac{-1}{(x+1)(x+h+1)}$ C) $\frac{h+2}{h(x+1)(x+h+1)}$ D) $\frac{1}{h^2}$ E) NOTA

14. Find the vertical, horizontal, and slant asymptotes, if any, for

$$f(x) = \frac{2x^3 + 15x^2 + 34x + 18}{x^2 + 5x + 4}$$

- A) vertical: x = -4, x = -1B) vertical: x = -4, x = -1C) vertical: x = 4, x = 1horizontal: y = 0slant: y = 2x 5slant: y = 2x 5
- D) vertical: x = -4, x = -1 E) NOTA slant: y = 2x + 5

NOTA = None of these answers

15. If the expression $px^3 + px + q$ is divided by x - 1, the remainder is 3. If it is divided by x + 1, the remainder is -7. What can be said about the coefficients of p and q?

A) they are positive and unequal numbers B) p = q C) p = 2.5 and q = 2 D) q = -2 and p can be any non-zero number E) NOTA

16. If r_1 and r_2 are the roots of the equation $ax^2 + bx + c = 0$, then $(r_1 - r_2)^2$ is equal to:

A)
$$\frac{b^2}{a^2}$$
 B) $\frac{b^2 - 4ac}{4a^2}$ C) $b^2 - 4ac$ D) $\frac{b^2 - 4ac}{a^2}$ E) NOTA
17. If $\frac{x^2}{9} - \frac{2}{3}x + 1 = 0$, then $\frac{x}{3}$ equals:
A) -3 B) 1 C) -2 D) 2 E) NOTA

18. If
$$y = \frac{\sqrt{(3x-5)(4x^2+12x+9)}}{6x^2-x-15}$$
 and $x > 2$, then y also equals:

A)
$$y = (3x-5)^{\frac{-1}{2}}$$
 B) $y = (3x-5)^{\frac{1}{2}}$ C) $y = \sqrt{\frac{1}{2x+3}}$ D) $y = \sqrt{\frac{2x+3}{3x-5}}$ E) NOTA

19. If
$$\log_8(\sqrt{a+x} + \sqrt{a-x}) + \log_8(\sqrt{a+x} - \sqrt{a-x}) = \frac{1}{3}$$
, find x.
A) -2 B) 2 C) 3 D) 8 E) NOTA

20. Find the sum of all of the real values of x for which $x^{\frac{2}{3}} - 3x^{\frac{1}{3}} = 4$

21. Solve
$$\frac{a^{x} - a^{-x}}{2} = 3$$
 for all real numbers x where $a > 0$.
A) $\log_{a}(3 \pm \sqrt{10})$ B) $\log_{a}(3 + \sqrt{10})$ C) $\log_{a}(3 \pm 2\sqrt{2})$

Theta Equations & Inequalities National Mu Alpha Theta Convention 2002 NOTA = None of these answers D) $\log_a \frac{1}{\sqrt{6}}$ E) NOTA 22. Given: x:y:z = 2:3:5, x + y + z = 100 and y = ax - 10Find a. C) 2.5 D) 3 A) 1.5 B) 2 E) NOTA 23. If $\frac{m}{n} = \frac{4}{3}$ and $\frac{r}{t} = \frac{9}{14}$ the value of $\frac{3mr-nt}{4nt-7mr}$ is: D) $\frac{11}{14}$ B) $\frac{-11}{14}$ A) -5.5 C) -1.25 E) NOTA 24. A mathematical ant finds that by crawling back 2" more from a vertical blade of grass its angle of elevation decreases from 45° to 30°. How high is the blade of grass? h A) √3 " B) $3 - \sqrt{3}$ C) $1 + \sqrt{3}$ <u>30°</u> 45° 2" D) $2-\sqrt{3}$ E) NOTA 25. If $y = \frac{10^{\log x}}{x^3}$, for x > 0, then which statement is true?

A) y varies directly with x
B) y varies directly as the cube root of x
D) y varies inversely with x²
E) NOTA

26. What is the circumference of the circle $x^2 + y^2 - 8x + 2y - 3 = 0$?

A) $2\pi\sqrt{5}$ B) $4\pi\sqrt{2}$ C) $4\pi\sqrt{5}$ D) 40π E) NOTA

- 27. What is the equation of the perpendicular bisector of the line segment whose endpoints are (3,5) and (-2,1)?
- A) -10x 8y + 29 = 0 B) 8x + 3y 13 = 0 C) 4x 3y + 7 = 0
- D) -6x + 4y 9 = 0 E) NOTA

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28. The longest chord possible to be drawn within $x^2 + 4y^2 - 2x - 24y - 19 = 0$ is what? A) $6\sqrt{14}$ B) $14\sqrt{2}$ C) $4\sqrt{14}$ D) $2\sqrt{14}$ E) NOTA 29. What is the y-intercept of the equation of the line given by $\begin{vmatrix} 1 & x & -1 \\ 2 & y & 3 \\ 3 & 2 & 1 \end{vmatrix} = 10$? A) (0, -6) B) (0, .5) C) (0, 5) D) $\left(0, \frac{-12}{11}\right)$ E. NOTA 30. Solve for x: $\begin{cases} xu = 400 \\ yv = 400 \\ x = 1.5y \\ v-u = 20 \end{cases}$ E) NOTA A) x = 10 B) x = 15 C) x = 20 D) x = 30 E) NOTA

31. Which of the following is the third term in the expansion of $(x^2 - 9)^{\frac{3}{2}}$?

A) $\frac{243}{8x}$ B) $\frac{-243}{8x}$ C) $\frac{-27x}{2}$ D) $\frac{27x}{2}$ E) NOTA

32. A boat takes two trips on a river. On the first trip, it travels upstream for 5 hours and returns in 2 hours. On the second trip it goes downstream for 3 hours, turns around and heads back upstream. After spending 7 hours on the return trip it is still 2 miles from its starting point. Which of the following is the speed of the current in miles per hours?

A) 3 B) 4 C) 6 D) 7 E) NOTA

33. If in $\triangle ABC$, $\angle C$ is a right angle, BC = 1 and tan $\angle B$ = p, find cos $\angle A$.

A) $\frac{1}{\sqrt{p^2 + 1}}$ B) $\frac{p}{p+1}$ C) $\frac{p}{\sqrt{p^2 + 1}}$ D) $\frac{\sqrt{p^2 + 1}}{p}$ E) NOTA

34. If $x = \sqrt{yz}$, x > 0, y > 0 and z > 0, then log y = ?

A) $\frac{x^2}{z}$ B) $\frac{2 \log x}{\log z}$ C) $2 \log x - \log z$ D) $2 (\log x - \log z)$ E) NOTA

NOTA = None of these answers

- 35. A teller totals his cash and finds q quarters, d dimes, n nickels, and p pennies. He later finds the x of his nickels were counted as quarters. Also, x of his dimes were counted as pennies. To correct his initial total he must:
- A) subtract 11 cents B) subtract 11x cents C) add 11 cents D) add 11x cents E) NOTA 36. If $(6x^2 + bx + 36) \div (2x + 7) = 3x + 5 + \frac{r}{2x + 7}$ find r + b. A) $\frac{-21}{2}$ B) 12 C) 31 D) 32 E) NOTA 37. If $6^{a+b} = 36$ and $6^{a+5b} = 216$ then a is equal to what? D) 7/ A) $\frac{1}{4}$ B) $\frac{3}{4}$ C) $\frac{5}{4}$ E) NOTA 38. Given $A = \begin{bmatrix} x & 6 & 2 \\ 0 & 1 & -5 \\ -2 & 3 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 3 & -1 \\ 1 & 4 \end{bmatrix}$. If Q = the value of x for which A is singular and R = the sum of the entries in B^2 , find the sum Q + R. B) 27 C) 45 D) 53 E) NOTA A) 19 39. How many of the following statements is/are always true about the function $f(x) = a^x$ where a > 0, and $a \neq 1$? 1) its domain is the positive real numbers 2) f(4) > f(-1)3) its graph has a y-intercept at (0,1) 4) its graph is asymptotic to the line y = 05) If $g(x) = \log_a x$, the f(g(x)) = xA) 1 B) 2 C) 3 D) 4 E) NOTA
- 40. The altitude to the base of an isosceles triangle is 8, while the perimeter is 32. What is the area of the triangle?

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NOTA = None of these answers		
A) 24	B) 32	

C) 40 D) 48 E) NOTA