



1. accept A, B, C, D
2. A
3. C
4. D
5. A
6. B
7. D
8. A
9. E, (2k)
10. A
11. C
12. B
13. C
14. D
15. C
16. C
17. B
18. A
19. B
20. D
21. D
22. E
23. E
24. D
25. A
26. C
27. A
28. B
29. A
30. D



1. **D**,  $\int_1^{e \cdot 5} \frac{dt}{t} = .5$ , which is equivalent to each of the answers.
2. **A**, for b, the expression is the average value of  $g(t)$ , and c is not necessarily true if  $G(x) < 0$  for any  $x$  on the interval.
3. **C**,  
 $\frac{dy}{y} = 3dx \rightarrow \ln y = 3x + C \rightarrow y = Ke^{3x}$   
 $1 = Ke^3 \rightarrow K = e^{-3} \rightarrow y(2) = e^{-3} \cdot e^6 = e^3$

4. **D**,  $\int_0^1 \frac{8x+4}{1+x^2} dx = 4\text{Arctan } x + 4\ln(1+x^2) \Big|_0^1 = \pi + 4\ln 2 = \ln(16e^\pi)$ .

5. **A**, calculation, we see:

$$\int_{\text{exact}} = 125 - 1 = 124.$$

$$\int_{\text{approx}} = 3 \cdot \frac{4}{8} (1 + 2 \cdot 4 + 2 \cdot 9 + 2 \cdot 16 + 25) = 126.$$

$$E = \text{approx} - \text{exact} = 2.$$

6. **B**,  $f(t) = t^2$ ;  $f(.5) = .25$ .

7. **D**,

$$f(t) = t^2; f'(t) = 2t$$

$$\text{Area} = \int_0^2 (2t - t^2) dt = \frac{4}{3}.$$

8. **A**, Becca's volume is  $\int_D (f(x))^2 dx$  while Skiya's volume is  $2 \left( \frac{\sqrt{3}}{4} \int_D (f(x))^2 dx \right) = \frac{\sqrt{3}}{2} \int_D (f(x))^2 dx$ . Clearly,

$$\int_D (f(x))^2 dx = \frac{\sqrt{3}}{2} \int_D (f(x))^2 dx.$$

9. **E**, Since each 'hump' of the  $\sin x$  curve has area 2, and the absolute value of  $\sin x$  from 0 to  $k\pi$  will have  $k$  'humps,' then the area must be  $2k$ .

10. **A**, T is the quarter-circle  $(a-1)^2 + (b-1)^2 = 2c$ , where  $a < 1$  and  $b > 1$ . The length is  $\frac{2\pi R}{4} = \frac{\pi\sqrt{2c}}{2}$ .

11. **C**,  $\ln(\sin 2x + 1) - \ln(\cos 2x) = \ln|\sec 2x + \tan 2x|$ ;  $\frac{d(\ln|\sec 2x + \tan 2x|)}{dx} = 2 \sec 2x$ .

12. **B**, definition of washer's method.



13. C,  $2\pi \int_1^2 (32 - 2x^4) dx = \frac{196}{5} \pi$ .

14. D,  $\frac{dy}{dx} = \frac{kx}{y} \rightarrow .5y^2 = .5kx^2 + C. \rightarrow k < 0 = \text{circle / ellipse}$   
 $k > 0 = \text{hyperbola} \rightarrow \text{NMI}$

15. C,  $\int f'(g(2x)) dx = f(g(2x)) + C \rightarrow 2g'(2x) = 1 \rightarrow$   
 $g(2x) = x + C; g(2x) = x + 8; g(4) = 2 + 8 = 10$

16. C,  $\int_1^2 x\sqrt{x-1} = 2 \int_0^1 (u^4 + u^2) du = \frac{16}{15}$ .

17. B,  $y = \cos(\sin^{-1}(\cos(\sin^{-1}(\cos(\dots))))))$   
 $\rightarrow y = \cos(\sin^{-1} y) = \sqrt{1 - y^2} \rightarrow y = \frac{1}{\sqrt{2}}$   
 $A = \frac{1}{\sqrt{2}}(\sqrt{2} - 0) = 1$

18. A, it is necessary but not sufficient.

19. B,  $\frac{f\left(\frac{\pi}{4}\right) - f\left(-\frac{\pi}{4}\right)}{\frac{\pi}{2}} = 0 = f'(c) = 0 \rightarrow p(c) = 0$

20. D,  $\int_0^{.25\pi} \tan \theta \cos \theta d\theta = \int_0^{.25\pi} \sin \theta d\theta = 1 - \frac{\sqrt{2}}{2}$

21. D,  $\lim_{n \rightarrow \infty} g(n) = \sum_{k=2}^{\infty} \frac{\ln k}{k}$ . Use integral test for convergence; the integral and therefore the limit does not exist.

22. B,

$$f(n) = \int_0^2 x \frac{n(n+1)}{2} dx = \frac{x \cdot 5n^2 + 5n + 1}{.5n^2 + .5n + 1} \Big|_0^2 = \frac{2 \cdot 5n^2 + 5n + 1}{.5n^2 + .5n + 1}$$

$$f(100) = \frac{2^{5051}}{5051}, f(99) = \frac{2^{5050}}{5050}; \frac{f(100)}{f(99)} = \frac{10100}{5051}$$

23. B,  $f(n) = g(n) \rightarrow \frac{f(100)}{g(99)} = \frac{f(100)}{f(99)} = \frac{10100}{5051}$ .



24. D,

$$A(t) = \frac{\int_0^{2t} v(x) dx}{t^2} \rightarrow \lim_{t \rightarrow 0} \frac{2v(2t)}{2t}; v(0) = 0$$
$$\rightarrow \lim_{t \rightarrow 0} \frac{2v'(2t)}{1} = 2v'(0) = 2a(0)$$

25. A,

$$\int e^x \ln x dx; u = e^x, du = e^x dx, dv = \ln x dx,$$
$$v = x \ln x - x \rightarrow \int e^x \ln x dx = e^x(x \ln x - x) -$$
$$\int e^x x \ln x dx + \int x e^x dx \rightarrow \int e^x \ln x(x+1) dx =$$
$$e^x(x \ln x - x) + x e^x - e^x = e^x(x \ln x - 1) \Big|_1^e =$$
$$e^e(e-1) + e$$

26. C,  $x = \frac{k}{n}$ ;  $width = \frac{1}{n} \rightarrow \frac{1}{\ln b} \int_0^3 b^x \ln b dx = \frac{b^3 - 1}{\ln b}$ .

27. E, The absolute value curves form a square of area 16. The smaller region is bounded by  $y = 2 - x$ ,  $y = 2$ , and  $x = 2$ . This has area of 2 (by simple geometry). Then the area of the big region is  $16 - 2 = 14$ .

28. B, if the axis of rotation is a side of the rectangle, a cylinder will be formed. Otherwise, a cylinder is not necessarily formed.

29. A,  $f'(x) = \cosh x; g'(x) = \sinh x;$   
 $f'^2 - g'^2 = 1 = y \rightarrow line$

30. D,  $f(T) = \text{Arc tan}(\sin T)$ , which is represented in the diagram by  $d$ .