



Mu Alpha Theta  
2006 National Convention

Alpha Bowl  
Answers

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|-------|------------|-------------|
| 1. 31 | 6. 33      | 11. 10,800  |
| 2. 80 | 7. 12      | 12. 13 / 12 |
| 3. 48 | 8. 10      | 13. -18     |
| 4. 0  | 9. $\pi/2$ | 14. 16      |
| 5. 5  | 10. -24    | 15. 12      |



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Solutions

<p>1. Impossible scores: 1,2,4,5,8,11   <math>\Sigma = \boxed{31}</math></p>	<p>2.  <math>\sin(\alpha + \beta) + \sin(\alpha - \beta)</math>  <math>= 2 \sin \alpha \cos \beta</math>  <math>\Rightarrow \alpha = 30^\circ, \beta = 10^\circ</math>  <math>2 \sin 30^\circ \cos 10^\circ = \cos 10^\circ</math>  <math>= \sin 80^\circ</math>  <math>\boxed{80}</math></p>	<p>3.  A: (-2, 1) B: (2,1)  C: (-6,-5) B: (6,-5)   ABCD is a trapezoid.   Area = <math>\frac{1}{2}(4 + 12)(6) = \boxed{48}</math></p>
<p>4.  <math>\sum_{n=1}^x k = \frac{x(x+1)}{2}</math>  <math>\sum_{n=1}^x k^3 = \left[ \frac{x(x+1)}{2} \right]^2</math>  <math>\sum_{n=1}^x k - \sqrt{\sum_{n=1}^x k^3} = \boxed{0}</math></p>	<p>5.  <math>\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta} = \frac{12}{5}</math>  <math>\frac{\sin 2\theta}{1 + \cos 2\theta} = \frac{\tan 2\theta}{\sec 2\theta + 1}</math>  <math>\sec 2\theta = \sqrt{\tan^2 2\theta + 1} = 13/5</math>  <math>(12/5) / (13/5 + 1) = 2/3</math>  <math>\rightarrow 2 + 3 = \boxed{5}</math></p>	<p>6.  A: 1 intersection (-3,0)  B: distance = <math>2c = 10</math>  C: length = <math>4p = 16</math>  D: area = <math>\pi ab = 6\pi</math>   A + B + C + D/<math>\pi</math> = <math>\boxed{33}</math></p>
<p>7.  A: <math>\Sigma = i - 1</math>  B: <math>\sqrt{8^2 + (-15)^2} = 17</math>  C: <math>-(2)(4)/2 = -4</math>  D: <math>1cis(-\pi/2) = -i</math>   A + B + C + D = <math>\boxed{12}</math></p>	<p>8.  A = 0  B = <math>\lim_{x \rightarrow 3} \frac{(x-3)(x^2-1)}{(x-3)(2x-5)} = 8</math>  C = -2  D = 4   A + B + C + D = <math>\boxed{10}</math></p>	<p>9. for <math>0 \leq \theta \leq 2\pi</math>  A = <math>(\pi/4, 5\pi/4)</math>  B = <math>(\pi/4, \pi/2) + (\pi, 5\pi/4)</math>  <math>+ (3\pi/2, 2\pi)</math>  A ∩ B = <math>(\pi/4, \pi/2)</math>  <math>+ (\pi, 5\pi/4)</math>  <math>\ell = (\pi/2 - \pi/4) + (5\pi/4 - 5\pi/4)</math>  <math>= \pi/4 + \pi/4 = \boxed{\pi/2}</math></p>
<p>10.  A = 5th term = <math>2^2 \binom{6}{2} = 60</math>  B = <math>(-3)(2)(1) = -6</math>  C = <math>8!/3! = 8</math>  D = <math>\binom{8}{2} = \frac{8!}{2!6!}</math>  BC/AD = <math>\boxed{-24}</math></p>	<p>11.  <math>(60)(360) = 21,600</math>  <math>2\pi r = 21,600</math>  <math>r = A/\pi</math>  <math>2A = 21,600</math>  A = <math>\boxed{10,800}</math></p>	<p>12.  A = <math>1/6 + 1/6 - 36 = 11/36</math>  B = <math>1/6 = 6/36</math>  C = <math>15/36</math>  D = <math>7/36</math>   A + B + C + D = <math>\boxed{13/12}</math></p>
<p>13. Multiplying by LCD leads to the system of equations:  A + B = 3  4A + B + C = 5  4A - 2B - C = 1  Solution (A,B,C) is (1,2,-1)  <math>\frac{9AB}{C} = \boxed{-18}</math></p>	<p>14.  A = Area = <math>4\sqrt{3}</math>  B = <math>(2)(\text{Area})/\text{Perimeter} = \frac{2\sqrt{3}}{3}</math>  C = <math>(4)(4)(4) / (4)(\text{Area}) = \frac{4\sqrt{3}}{3}</math>  D = <math>\text{Area}/(\text{Perimeter}/2) = \frac{2\sqrt{3}}{3}</math>   <math>\frac{A \cdot B \cdot C}{D} = \boxed{16}</math></p>	<p>15.  A = <math>15^\circ</math>, B = <math>90^\circ</math>  <math>\sin 105^\circ = \sin(60^\circ + 45^\circ)</math>  <math>\sin 60^\circ \cos 45^\circ + \sin 45^\circ \cos 60^\circ</math>  <math>= \frac{\sqrt{2} + \sqrt{6}}{4}</math>   <math>\rightarrow 2 + 4 + 6 = \boxed{12}</math></p>