

# Alpha Ciphering

Mu Alpha Theta 2006 National Convention



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Question # P

Simplify the following expression into a single trigonometric function

$$\frac{1}{2}(\cos \theta + \sin \theta)(\csc \theta - \sec \theta)$$



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**Question # 1**

Evaluate  $8(\sin^2 x)(\cos x) + \tan^2 x$  if  $x = \frac{\pi}{3}$ .



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**Question # 2**

Two consecutive positive integers  $a$  and  $b$  exist such that  $a^2 - b^2 = 101$ . What is the value of  $a$ ?



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Question # 3

Solve for  $x$  over the set of real numbers:

$$\sqrt{x^4 + x^4 + x^4 + x^4} = 4$$



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Question # 4

Find the volume of the solid generated by revolving a rectangle with vertices  $(2,2)$ ,  $(2,5)$ ,  $(5,2)$  and  $(5,5)$  about the  $y$ -axis.



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Question # 4

Find the volume of the solid generated by revolving a rectangle with vertices  $(2,2)$ ,  $(2,5)$ ,  $(5,2)$  and  $(5,5)$  about the  $y$ -axis.



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**Question # 5**

Solve for  $x$ :  $(2 + 2i)^8 = 4^x$ , where  $i = \sqrt{-1}$



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Question # 6

What is the sum of all integers which belong to the domain of

$$f(x) = \frac{2x}{\sqrt{7x - x^2 - 10}} ?$$



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Question # 7

If  $\tan \alpha = \frac{4}{3}$ , where  $\alpha$  is in quadrant III, and if  
 $\cos \beta = \frac{-7}{25}$ , where  $\beta$  is in quadrant II, evaluate  
 $\sin(\alpha - \beta)$ .



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**Question # 8**

A pinochle deck consists of 48 cards. There are 6 different face values (nine, ten, jack, queen, king, and ace), 4 different suits (clubs, diamonds, hearts, and spades), and there are 2 of each card in the deck. Two cards are drawn at random from the deck without replacement. If  $P$  = the probability that the cards have the same face value, and  $Q$  = the probability that the cards are the same suit, find  $P + Q$ .



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Question # 9

Evaluate:  $\lim_{x \rightarrow 4} \left( \frac{2x-8}{x^2-3x-4} + \frac{x-4}{\sqrt{x}-2} \right)$



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Question # 10

Given the equation  $2e^{2x} + \frac{30}{e^{2x}} = 17$ . If the sum of all real solutions to this equation is equal to  $\ln p$ , then what is the value of  $p$ ?



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Given that  $k$  is a positive real number, find (in terms of  $k$ ) the area of the region bounded by the equation  $|x| + |y| = k$ .



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Question # 12

$$\text{If } \frac{A}{x-2} + \frac{B}{x-4} = \frac{8x-26}{x^2-6x+8},$$

then find the value of  $A^B$ .



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