



**Mu Alpha Theta
2006 National Convention**

**Theta Ciphering
Answers**

P. $-2\frac{2}{3}$

1. 4

2. 6720

3. $\frac{-14}{5}$ or 2.8

4. 30π

5. 23

6. 0

7. 104

8. 3

9. 92

10. $\frac{139}{81}$

11. 2

12. $\frac{1}{12}$



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**Theta Ciphering
Solutions**

1. $(2x+3)(x-4) = 0$, so $x = -3/2$ or $x = 4$.
ANSWER: 4

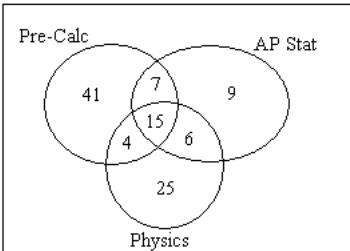
2. $\frac{8!}{3!} = \frac{40320}{6} = 6720$ **ANSWER: 6720**

3. $2^{2(2x-1)} = 2^{3(3x+4)}$ so $2(2x-1) = 3(3x+4)$
 $4x-2 = 9x+12$ so $-14 = 5x$
 $x = \frac{-14}{5}$ or -2.8 **ANSWER: $\frac{-14}{5}$ or 2.8**

4. $36(x-1)^2 + 25(y-5)^2 = 900$
 $\frac{(x-1)^2}{25} + \frac{(y-5)^2}{36} = 1$

Area of ellipse = $\pi ab = \pi(\sqrt{36})(\sqrt{25}) = 30\pi$
ANSWER: 30π

5.



$130 - 41 - 7 - 9 - 15 - 4 - 6 - 25 = 23$

ANSWER: 23

6. The determinant of a matrix and the determinant of the transpose of the matrix are equal
ANSWER: 0

7. $1008 = 2^4 \cdot 3^2 \cdot 7$

odd factors are 1, 3, 7, $(3)(3) = 9$,
 $(3)(7) = 21$, and $(3)(3)(7) = 63$

$1 + 3 + 7 + 9 + 21 + 63 = 104$ **ANSWER: 104**

8. $|3x-5| \leq 11$ $|2x+1| > 5$
 $-11 \leq 3x-5 \leq 11$ $2x+1 > 5$ or $2x+1 < -5$
 $-6 \leq 3x \leq 16$ $2x > 4$ or $2x < -6$
 $-2 \leq x \leq \frac{16}{3}$ $x > 2$ or $x < -3$

The only integers the two solution sets share are 3, 4, and 5 **ANSWER: 3**

9.
$$\frac{2}{(1+\sqrt{3})+\sqrt{5}} \left(\frac{(1+\sqrt{3})-\sqrt{5}}{(1+\sqrt{3})-\sqrt{5}} \right) =$$

$$\frac{2+2\sqrt{3}-2\sqrt{5}}{(1+2\sqrt{3}+3)-5} = \frac{2+2\sqrt{3}-2\sqrt{5}}{-1+2\sqrt{3}}$$

$$\frac{2+2\sqrt{3}-2\sqrt{5}}{-1+2\sqrt{3}} \left(\frac{-1-2\sqrt{3}}{-1-2\sqrt{3}} \right) =$$

$$\frac{-2-2\sqrt{3}+2\sqrt{5}-4\sqrt{3}-12+4\sqrt{15}}{1-12} =$$

$$\frac{-14-6\sqrt{3}+2\sqrt{5}+4\sqrt{15}}{-11} =$$

$$= \frac{14+6\sqrt{3}-2\sqrt{5}-4\sqrt{15}}{11}$$

$$A = 14, B = 6, C = -2, D = -4; AB + CD = 84 + 8 = 92$$
ANSWER: 92

10. First 4 terms:

$$(1)^{\frac{1}{3}} + \frac{1}{3}(1)^{\frac{-2}{3}}(2)^1 - \frac{1}{9}(1)^{\frac{-5}{3}}(2)^2 + \frac{5}{81}(1)^{\frac{-8}{3}}(2)^3 =$$

$$1 + \frac{2}{3} - \frac{4}{9} + \frac{40}{81} = \frac{139}{81}$$
ANSWER: $\frac{139}{81}$

11. Use quadratic formula:

$$x^2 = \frac{5 \pm \sqrt{25 - 4(3)(C)}}{2(3)}$$

For real roots, discriminant $25 - 4(3)(C) \geq 0$

$C \leq \frac{25}{12}$; largest integer which satisfies equation is 2 **ANSWER: 2**

12. Only 4 restaurants remain for Tuesday, 3

remain for Wednesday; $P = \left(\frac{1}{4}\right)\left(\frac{1}{3}\right) = \frac{1}{12}$

ANSWER: $\frac{1}{12}$