



Mu Alpha Theta  
2006 National Convention

Logs and Exponents  
Theta Division

1. Find the largest integral value of  $x$  for which  $5^{x+2} < 5^x + 5$ .

A. -2      B. -1      C. 0      D. 1      E. NOTA

2. Given:

$$A = \left(2^{-1} - 3^{-1}\right)^{-1}$$

$$B = \left(\frac{1}{2} + \frac{1}{3}\right)^{-1}$$

$$C = \left[3\sqrt{125} - 2\sqrt{45} - \sqrt{80}\right]^2 \quad \text{Find: } \frac{ABC}{D}.$$

$$D = (3\sqrt{5} + 3)(3\sqrt{5} - 3)$$

A.  $\frac{50}{9}$       B. 5      C.  $\frac{100}{9}$       D. 25      E. NOTA

3. Solve for  $y$ : ( $x > 0, x \neq 1$ )  $\left[\frac{x^{3k-2}}{x^{2k+1}}\right] \left[\frac{x^{k-3}}{(x^{k+1})^2}\right] = x^y$

A.  $k - 7$       B.  $k - 4$       C.  $k - 3$       D. -8      E. NOTA

4. Given:  $\log A = 2.5$ ,  $\log B = 1.2$ ,  $\log C = 3.6$       Find:  $\log \frac{10A}{B} + \log \frac{A^3}{100C}$

A.  $\frac{8}{5}$       B.  $\frac{21}{10}$       C.  $\frac{21}{5}$       D.  $\frac{47}{10}$       E. NOTA

5. If  $x^{x^3} = 3$ , what is the value of  $x$ ?

A. 1      B. -1      C.  $\sqrt[3]{3}$       D.  $\sqrt[3]{\frac{1}{3}}$       E. NOTA

6. If  $2^{x-3} = 1$ , and  $5^{y+2} = 1$ , what is the value of  $2^x 5^y$ ?

A.  $\frac{4}{25}$       B.  $\frac{8}{25}$       C.  $\frac{4}{5}$       D.  $\frac{8}{5}$       E. NOTA

7. Solve for  $x$ :  $\log_2(x+1) = 2\log_2(x-1)$ .

A. 0, 3      B. 0      C. 1      D. 3      E. NOTA



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8. Evaluate  $2(\log_8 12) - \frac{1}{2}(\log_8 81)$ .
- A.  $\frac{4}{3}$       B.  $\frac{8}{3}$       C. 4      D. 8      E. NOTA
9. If  $t > 0$  and  $a = \frac{b}{(1+t)^x}$ , then  $x$  equals
- A.  $\log\left[\frac{b}{(a(1+t))}\right]$       B.  $\frac{\log\left(\frac{b}{a}\right)}{\log(1+t)}$       C.  $\log\left[\frac{b-a}{(t+1)}\right]$       D.  $\log\left(\frac{b}{a}\right) - \log(1+t)$       E. NOTA
10. Given  $\log 2 = 0.301$ , and  $\log 3 = 0.477$ . Find  $\log (0.75)$ .
- A. 0.8751      B. -0.1078      C. -0.125      D. -1.078      E. NOTA
11. If  $2^x = 4^{y+1}$ , and  $x^2 = (y+1)^4$ , find the sum of the possible values of  $x$ .
- A. 0      B. 2      C. 4      D. infinite      E. NOTA
12. A function is defined on the set of positive integers as follows:
- $$M(n) = \begin{cases} \log p & \text{if } n=p^m \text{ for some prime } p \text{ and some integer } m \geq 1 \\ 0 & \text{otherwise} \end{cases}$$
- Calculate  $M(4) + M(6) + M(9)$
- A)  $\log 2$       B)  $\log 3$       C)  $\log 6$       D) 0      E) NOTA
13. Given that  $\log 2 = a$ ,  $\log 5 = b$ , and  $\log 7 = c$ , then  $\log \frac{50}{7}$  can be expressed as:
- A)  $\frac{ab^2}{c}$       B)  $\frac{a+2b}{c}$       C)  $a+2b-c$       D)  $ab^2-c$       E) NOTA
14. Reduce to lowest terms:  $\frac{9^{x+2}}{(3^{x-1})^x} \div \frac{(27^x)^{x+1}}{81^{x^2-1}}$
- A) -1      B) 0      C) 1      D) 3      E) NOTA
15. The base 3 logarithm of  $(9\sqrt{27})(\sqrt[3]{3})$  is what?
- A)  $\frac{10}{3}$       B)  $\frac{23}{6}$       C)  $\frac{17}{6}$       D)  $\frac{16}{3}$       E) NOTA



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16. Simplify:  $\left[ 27^{\frac{2}{3}} + 64^{\frac{2}{3}} \right]^{\frac{3}{2}} - 10^2$
- A) -9      B) 25      C) 191      D) 225      E) NOTA
17. Solve for x if  $8^{3x+2} = 4^{5x-1}$
- A) 1      B) 2      C) 4      D) 8      E) NOTA
18. If  $3^x + 3^{-x} = \frac{10}{3}$ , the sum of the possible solutions is:
- A) -2      B) 0      C) 2      D) 3      E) NOTA
19. Solve:  $6x^{\frac{-1}{2}} - 17x^{\frac{-1}{4}} = -5$
- A.  $\left(\frac{1}{3}, \frac{5}{2}\right)$       B.  $\left(\frac{2}{5}, 3\right)$       C.  $\left(\frac{16}{625}, 81\right)$       D.  $\left(\frac{1}{81}, \frac{625}{16}\right)$       E. NOTA
20. If  $x = (\log_9 3)^{\log_2 16}$ , then  $\log_4 x =$
- A. -2      B.  $\frac{1}{2}$       C.  $-\frac{1}{2}$       D. 2      E. NOTA
21. If  $\ln x^2 = (\ln x)^2$ , then x equals
- A. 1      B.  $e$       C.  $1, e$       D.  $1, e^2$       E. NOTA
22. If  $A = \log_8 225$  and  $B = \log_2 15$ , then the ratio of A to B is
- A. 2:8      B. 8:2      C. 2:3      D. 3:2      E. NOTA
23. If  $\frac{e^x + e^{-x}}{e^x - e^{-x}} = 2$ , find x.
- A.  $\frac{1}{2} \ln 3$       B.  $\frac{1}{3} \ln 2$       C.  $\ln 2$       D.  $\ln 3 - \ln 2$       E. NOTA



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24. Find the greatest integer  $x$  for which  $3^{20} > (32)^x$ .
- A. 5      B. 6      C. 7      D. 8      E. NOTA
25. If  $\ln x^4 = (\ln x)^3$ , find  $x$ .
- A.  $e^2, \frac{1}{e^2}, 1$       B.  $e^2, \frac{1}{e^2}, e$       C.  $e^3, \frac{1}{e^3}, 1$       D.  $e^3, \frac{1}{e^3}, e$       E. NOTA
26. If  $\log_b 2 = 0.2789$ ,  $\log_b 3 = 0.4421$  and  $\log_b 7 = 0.7831$ , find  $\log_b \frac{14}{3b}$ .
- A. -0.3801      B. 0.7364      C. 0.6199      D. 0.5119      E. NOTA
27. Solve for  $x$ :  $\ln(x-2) - 1 = \ln(x+2)$ .
- A.  $\frac{2+2e}{1-e}$       B.  $\frac{2+2e}{1+e}$       C.  $\frac{2-2e}{1+e}$       D.  $\frac{2-2e}{1-e}$       E. NOTA
28. Solve for  $(x, y)$
- $$\begin{cases} \log_y(9-4x) = 1 \\ \log_{4+2y} 3x = 1 \end{cases}$$
- A.  $(2, -1)$       B.  $(2, 1)$       C.  $(-3, 1)$       D.  $\emptyset$       E. NOTA
29. Find the sum of the roots of the equation:  $8e^x + \frac{27}{e^x} = 35$ .
- A.  $\frac{-35}{8}$       B.  $\ln \frac{27}{8}$       C.  $\ln \frac{35}{8}$       D.  $\frac{27}{8}$       E. NOTA
30. For all positive numbers  $x$  distinct from 1,  $\frac{1}{\log_3 x} + \frac{1}{\log_4 x} + \frac{1}{\log_5 x} =$
- A.  $\frac{1}{\log_{60} x}$       B.  $\frac{1}{\log_x 60}$       C.  $\frac{1}{(\log_3 x)(\log_4 x)(\log_5 x)}$       D.  $\frac{12}{(\log_3 x)(\log_4 x)(\log_5 x)}$       E. NOTA