

If a and b are the solutions of the given equation, find $|a - b|$.

$$\begin{vmatrix} x & 1 \\ x & 2x \end{vmatrix} = 3$$

Find the y -intercept of a line that has an x -intercept of 2 and is perpendicular to the line containing the points $(-2,3)$ and $(3,5)$.

If $\frac{4 - 3i}{2 + i}$ is written in the form $a + bi$ (where $a, b \in \Re$ and $i = \sqrt{-1}$),

find the sum $|a| + |b|$.

Find all real values of k such that the graph of $y = x^2 + 2kx + k$ does not intersect the x -axis.

Given: y varies directly as x and inversely as the square of z
 $y = 2$ when $x = 3$ and $z = 4$

Find y when $x = 9$ and $z = 2$.

A rectangle is inscribed in an ellipse with equation $9x^2 + 25y^2 - 225 = 0$ in such a way that the foci of the ellipse lie on the rectangle. Find the area of this rectangle.

Solve over \mathfrak{R} : $\log_5(x-1) + \log_5(x-2) = \log_5(x+6)$

A line is tangent to the circle with equation $x^2 + y^2 - 6x + 4y - 12 = 0$ at the point on the circle in the fourth quadrant where $x = 7$. Find the equation of the tangent line in the form $y = mx + b$.

Find the numerical value of $\frac{x^4 - x^3 + x - 1}{x^3 - 2x^2 + 2x - 1}$ when $x = 2008$.

An alloy of gold and silver is 25% gold. To obtain an alloy that is 40% gold, 12 pounds of the old alloy must be removed and replaced by pure gold. Find the weight, in pounds, of the old alloy.

Find the sum of all the x and y coordinates of all points of intersection of the graphs of $x^2 + 2y^2 = 54$ and $2x - y = -9$.

A box contains 40 tickets numbered 1, 2, 3, 4, ..., 40. If two tickets are drawn without replacement, find the probability that the sum of their numbers is even.