

1. **B.** $(x-1)^2 + (x+1) = x^2 - 2x + 1 + x - 1 = x^2 - x$.
2. **C.** $e^{-2x} \neq e^{2x}$ for any x except 0.
3. **C.** Since $\sec(x)$ is $1/\cos(x)$ and $\cos\left(\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2}$ then $\sec(x) = \frac{2}{\sqrt{2}}$ and squaring this gives $4/2=2$.
4. **B.** Changing to standard form, we get $4x-3y=9$. The distance from a point to a line is $\frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}}$
 which gives $\frac{|0 - 3(5) - 9|}{\sqrt{4^2 + 3^2}} = \frac{24}{5}$.
5. **B.** $f(10) = 4^{11} = 2^{22}$ and $g(12) = 2^{11}$ and the product is $2^{22} \cdot 2^{11} = 2^{33}$ so $k = 33$.
6. **A.** $y = \sqrt{1 - \left(x - \frac{\pi}{2}\right)^2}$ is the top half of the graph of $y^2 + \left(x - \frac{\pi}{2}\right)^2 = 1$ which is a circle of radius 1 and center $\left(0, \frac{\pi}{2}\right)$. The max point is $\left(\frac{\pi}{2}, 1\right)$. $y = \sin(x)$ has the same max point.
7. **D.** $\sqrt[3]{x+1} = 2$; $x+1 = 8$ so $x=7$.
8. **D.** $f\left(-\frac{1}{3}\right) = -3$ by the first part of the function, and $f(-3) = \frac{1}{2} + \frac{-1}{3} = \frac{1}{6}$ by the second part of the function.
9. **B.** f is always 9.
10. **B.** $f(x) = \sqrt{x+2} + (x+2)$ so $f(14) = f(16-2) = 4+14=20$ and $f(7) = f(9-2) = 3+9=12$. The difference is 8.
11. **C.** The right hand side of the equation is 1 since $\sin\frac{\pi}{4} = \cos\frac{\pi}{4}$. So the equation $\sin x + \cos x = 1$ is true for choice C.
12. **C.** The coefficient of the 3rd term is $C(10, 2)$ which is $\frac{10!}{2!8!}$ and the coefficient of the 9th term is $C(10, 8)$ which is the same. So the quotient is 1.
13. **C.** $f(7) = \sqrt{8+2\sqrt{7}} = \sqrt{(\sqrt{1}+\sqrt{7})^2} = 1+\sqrt{7}$. So $1(7)=7$.
14. **B.** $\log k + \log(k+2) = \log 48 - \log 2$ $\log k(k+2) = \log 24$, $k^2 + 2k = 24$
 so $k^2 + 2k - 24 = 0$, $(k-4)(k+2) = 0$ so $k=4$ and $\log_2\left(\frac{1}{4}\right) = -2$.
15. **A.** The angles are 101, 101+d, 101+2d, ..., 101+6d. The sum is $180(7-2)=900$. $707+21d=900$. $21d=193$, so largest angle is $101+6(193/21)$ is 156 to the nearest degree. The sum of the digits is 12.
16. **C.** The sum of the roots of f is 3. The sum of the roots of g is 10. So the missing root must be $10-3=7$.
17. **C.** The smallest number of integral factors for c^n is $(n+1)$. Since c cannot be 2 (x is odd) then the smallest value for c is 3. 3^4 has five factors: 1, 3, 9, 27, 81.
18. **B.** The probability of at least one heads is the same as 1 minus the probability of no heads. So $P(2) = 1 - 1/4 = 3/4$. $P(3) = 1 - 1/8 = 7/8$ and $P(n) = \frac{2^n - 1}{2^n}$ and since this is greater than $15/16$, we get $2^n > 16$ and so $n > 4$. Since n is an integer (flips of coins), $n=5$.
19. **A.** $f(10)$ means there are 20 people and we want the seat opposite to seat 10. Pattern: for four seats, opposite seat 1 is seat 3 and in general, opposite seat n is seat $(n+2)$. For six seats, opposite seat n is

seat $(n+3)$ and for twenty seats, opposite seat n is seat $(n+10)$. So opposite seat 10 is seat 20.
 20. **D.** f and g are inverses so their composite is equal x , so $f(g(1))=1$.

21. **D.** $f(x) = 16cis\left(-\frac{\pi}{4}\right)$ and $\left(16cis\left(-\frac{\pi}{4}\right)\right)^{\frac{1}{4}} = 2cis\left(-\frac{\pi}{16}\right)$ by DeMoivre's Theorem. Each fourth root occurs at intervals of $\frac{2\pi}{4} = \frac{\pi}{2}$ and since $2\pi + \frac{-\pi}{16} = \frac{31\pi}{16}$, and angles for the other roots are $\frac{21\pi}{16}, \frac{15\pi}{16}, \frac{7\pi}{16}$.

22. **A.** $f(g(x)) = \frac{\sqrt{(x^2-1)-1}}{(x^2-1)^2-4}$ so $(x^2-1)-1$ must be ≥ 0 and $x^2 \geq 2$ so $|x| \geq \sqrt{2}$. Then $(x^2-1)^2-4 \neq 0$ and $(x^2-1)^2 \neq 4$ and $x^2-1 \neq \pm 2$ so $x^2 \neq 3, x^2 \neq -1$ so $x \neq \pm\sqrt{3}$. This gives domain $(-\infty, -\sqrt{3}) \cup (-\sqrt{3}, -\sqrt{2}] \cup [\sqrt{2}, \sqrt{3}) \cup (\sqrt{3}, \infty)$.

23. **A.** $f(t) = \frac{200}{1+e^{-0.1t}} = \frac{200\sqrt{e}}{1+\sqrt{e}}$ and cross multiply to get $\sqrt{e} + e^{\frac{1}{2} \cdot \frac{1}{10}t} = 1 + \sqrt{e}$ so $e^{\frac{1}{2} \cdot \frac{1}{10}t} = 1$ when the exponent is 0 or when $t=5$. This is 5 hours after midnight. 5 AM.

24. **B.** $(\log_4 25)(3\log_5 2) = \left(\frac{2\log 5}{2\log 2}\right)\left(\frac{3\log 2}{\log 5}\right) = 3$

25. **C.** $f(20)=12$ means 20 people were surveyed and 12 liked coffee and 18 liked tea. $12+18=30$ so 10 were counted twice.

26. **C.** The sum is the first bounce plus the sum of an infinite series.

$$x + \frac{4}{5}(2x) + \frac{16}{25}(2x) + \dots = x + \frac{a_1}{1-r} = x + \frac{\frac{4}{5}(2x)}{1-\frac{1}{5}} = x + 8x$$

Getting $9x=7200$ gives the initial height x is 800.

27. **D.** The $\arctan(x)$ function has asymptotes at $x=\pi/2$ and $x=-\pi/2$.

28. **D.** At $t=1, D=0.5$; at $t=2, D=1$, and at $t=n, D=n/2$. The centers are 12 units apart when the circles are tangent to each other. So at $t=24, D=12$ and $D(24)=12$.

29. **B.** $\sqrt{x^2-2x+1} = \sqrt{(x-1)^2} = |x-1|$ and when $x < 1$, $f(x) = -(x-1) = 1-x$. $f(a)-f(b) = (1-a)-(1-b) = b-a$.

30. **D.** The possible products for $f(2), f(3)$ are

a, b	a*b	a, b, c	a*b*c
2, 4	8	2, 4, 6	48
2, 6	12	2, 4, 8	64
2, 8	16	2, 4, 16	128
2, 16	32	2, 6, 8	96
4, 6	24	2, 6, 16	192
4, 8	32	2, 8, 16	256
4, 16	64	4, 6, 8	192
6, 8	48	4, 6, 16	384
6, 16	96	4, 8, 16	512
8, 16	128	6, 8, 16	768

The only ways $f(2) > f(3)$ are
 $64 >$ one prod. $96 <$ two prod.
 $128 <$ three products $6/100 = 3/50$

