1. A	7. D	13. C	19. A	25. D
2. D	8. D	14. D	20. D	26. E
3. B	9. E	15. C	21. E	27. B
4. D	10. D	16. A	22. B	28. C
5. A	11. B	17. B	23. D	29. D
6. B	12. A	18. A	24. A	30. C

The following were changed at the resolution center at the convention: 8 B, 9 D, 17 E, 20 E, 22 E Solutions: Functions with Pre Calc Apps

1. A.
$$\frac{(7a-2)-(7b-2)}{a-b} = \frac{7(a-b)}{a-b} = 7$$

2. D. f is a line with positive slope; g is a line with negative slope; h is a line with 0 slope; k is a line with positive slope. f and k are increasing.

3. **B**.
$$f^{-1}(x): x = \frac{2y-5}{3}$$
 solves to $y = \frac{3x+5}{2}$

- 4. D.
- 5. A. Substituting shows that all three points line on the curve in choice A.
- 6. B. An even function has the property that f(-x) = f(x) for all x, and even powers are a clue to some even functions. II and IV do not change for f(-x). Choice A has $f(-x) = (-x-9)^2 + 4$ and for x= -1 we see a different answer than x=1.

7. D. Let x=3:
$$f(3) = \frac{f(1)}{f(2)}$$
=10. Let x=5:

$$f(5) = \frac{f(3)}{f(4)} = 20$$
 so $\frac{10}{f(4)} = 20$ and
 $f(4) = 1/2$. So f(3), f(4), f(5) are

10, 1/2, 20 and by the formula, we can multiply two consecutive terms to get the term previous to both. So f(2)=5, f(1)=50, f(0)=250. Then we have the sequence 250, 50, 5, 10, 1/2, 20 and we can verify each term by letting x=0 through x=5 or further. f(0)=250.

8. D. D. Divide to get
$$\frac{(y-1)^2}{B} - \frac{(x+2)^2}{4}$$

$$\frac{(x+2)^2}{B} - \frac{(x+2)^2}{4} = 1$$

which has asymptotes with slope $\frac{\nabla D}{2}$.

Since this is equal to 3/4 (original line given) then we have B=9/4.

9. E. Since 3 times each term of f does not give g, A is not true. Similarly adding 3 to f does not give g, so B is not true. For c, we consider $(x-3)^3 - 10(x-3)^2 + 27(x-3) - 18$ and let x=3. This gives for C, f(3)= -18. But g(3)= 27-90+27-18, not -18. So C is not true.

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Similarly D is not true, and the answer is E.

10. D.
$$g(x) = -\sqrt{x-1}$$
 and f and g are shown.

As x increases
the
$$g(x)$$
 decreases
so A is false.
g has domain
 $[1, \infty)$ and $g(1)$ =
 $f(0)$ =1. D is true.

11. B. Knowing that the vertex is at (-1, 0), we need to find f(-2) and f(2), and they are

1 and 9 respectively. So the range is [0, 9].

- 12. A. When the sine is 1, we have the maximum. The period of this graph is $2\pi/(160\pi)$ =
 - 1/80. From x=0 to 1/80, we have 1 max point. 1 max п

So
$$\frac{1}{1/80} = \frac{1}{1}$$
 and so n=80.

- 13. <u>C</u>. Since x=5 makes f undefined and g has domain x > -4, the intersection is C.
- 14. **D**. When x and y are substituted by -xand -y, we should get an opposite answer. Since choice C has odd powers, $(-x) + (-y)^3$

$$= -(x + y^{3}).$$

15. **c**. $3\ln(e^{5}) - 1 = 3(5) - 1 = 14.$

- 16. <u>A</u>. When x=1/2, $3x^{3/2} \frac{\sqrt{x+1}}{|x-2|} \le x$
- (simplified) gives $\frac{3}{2\sqrt{2}} \frac{\sqrt{3/2}}{3/2} =$ $\frac{3\sqrt{2}}{4} - \frac{1}{\sqrt{3/2}} = \frac{3\sqrt{2}}{4} - \frac{\sqrt{2}}{\sqrt{3}} = \frac{3\sqrt{2}}{4} - \frac{\sqrt{6}}{3}$ $=\sqrt{2}(\frac{3}{4}-\frac{\sqrt{3}}{3})\approx 1.4$ (.75-1.7/3) ≈ 1.4 (.75-.6)

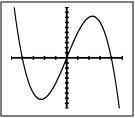
17. B. Since sine has range [-1, 1], the range of f is -4 ± 1 .

18. A.
$$x(x-4)(x+4) \neq 0$$
.

19. **A**.
$$\sqrt{3^2 + 3^2} = 3\sqrt{2}$$

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- 20. <u>D</u>. For Choice A, if b=2, $(a+5) \ge 0$. True. For Choice B, if b= -6, then $(a+5) \le 0$, True. For Choice C, if b= -4, then $(a+5) \le 0$, True. For Choice D, if b= -2, then $(a+5) \le 0$, False. The answer is then **D**.
- 21. <u>E.</u> Phase shift is $-1/\pi$.
- <u>B.</u> The equation has roots at -4, O and 4. Knowing the shape of the graph, we see that over that interval,



the value is negative after x=4. So only at x=5 and x=6 do we have negative values.

23. <u>D</u>. The slope of an asymptote is 3/4 and putting the conic in the form

$$\frac{(y-1)^2}{B} - \frac{(x+2)^2}{4} = 1$$
 gives the slope of asymptotes $\frac{\sqrt{B}}{2}$. Setting this equal to 3/4

gives B= 9/4.

24. <u>A</u>. The sum of the two irrational roots is 3 and the product is 7, so $x^2 - 3x + 7$ is a factor of f. Multiply by (x-4) to get choice A.

25. D.
$$\cos(\Omega + \phi) = \cos\Omega\cos\phi - \sin\Omega\sin\phi$$

 $=\frac{24}{25} \frac{4}{5} - \frac{7}{25} \frac{3}{5} = \frac{75}{125} = \frac{3}{5}.$

26. <u>E</u>. The polynomial factors to $(x+2)^3(x+4)$ so the distinct roots are -2 and -4.

27. <u>B</u>. Let the roots be a, -a and b. The sum of the roots is then b, and since -B/A (coefficients) gives the sum is -3, then b= -3. The product of the roots is E/A=-12, then $-3a^2 = -12$ gives the other roots are 2 and -2. For x= any of these roots, set the polynomial =0 to get k= -4.

28. C. Sec(3x)=
$$\sqrt{2}$$
 for $\frac{\pi}{4}$ and $\frac{7\pi}{4}$,
 $2\pi + \frac{\pi}{4}$ and $2\pi + \frac{7\pi}{4}$, and $4\pi + \dots$

Since is equal to 3x, we get x=

$$\frac{\pi}{12}, \frac{7\pi}{12}, \frac{9\pi}{12}, \frac{15\pi}{12}, \frac{17\pi}{12}, \frac{23\pi}{12}$$
. Sum is 6π .
29. D. $y = \frac{(2x+1)(x+5)}{(x+12)(x-10)}$ has vertical

asymptotes where the function is undefined. At x=-12, x=10, choice D.

30. <u>C</u>. The sum of the zeros is -B/A = 1/2.