

Answers:

1.  $\sim q \rightarrow p$
2. 13
3.  $4\sqrt{2}$
4.  $54^\circ$
5.  $30^\circ$
6. F or False
7. 10
8.  $170^\circ$
9. 7
10.  $13^\circ$
11.  $100^\circ$
12. 325
13.  $3\sqrt{14}$
14. 41
15. 16
16.  $2 + \sqrt{6}$
17.  $\frac{\pi}{6}$  or  $\pi:6$
18.  $\frac{1}{\pi}$  or  $1:\pi$
19.  $\frac{1}{3}$  or  $1:3$
20. 4
21.  $38\sqrt{3}$
22.  $64\pi$
23.  $2\sqrt{10}$
24.  $\frac{1}{3}$  or  $1:3$
25.  $\frac{36}{5}$

Solutions:

1. Contrapositive is  $q \rightarrow \sim p$ , inverse of that is  $\sim q \rightarrow p$ .
2. Third side must be 3, 4, 5, 6, or 7, but to be the largest, it would have to be 6 or 7.  
 $6+7=13$
3.  $x^2 = 4(12-4) = 4 \cdot 8 = 32 \Rightarrow x = 4\sqrt{2}$
4. Exterior angle has measure  $\frac{360^\circ}{10} = 36^\circ$ , complement is  $54^\circ$
5.  $CD = 2 \cdot 80^\circ = 160^\circ$ ,  $DB = 360^\circ - 160^\circ - 100^\circ = 100^\circ \Rightarrow \angle CAD = \frac{1}{2}(160 - 100)^\circ = 30^\circ$
6.  $p, q$  T &  $r$  F  $\Rightarrow p \wedge q$  T  $\Rightarrow p \wedge q \rightarrow r$  F
7.  $x^2 + 8x = 180 \Rightarrow x^2 + 8x - 180 = 0 \Rightarrow (x+18)(x-10) = 0 \Rightarrow x = 10$
8.  $(1+2+\dots+8)x = 360 \Rightarrow 36x = 360 \Rightarrow x = 10$  is smallest exterior angle  $\Rightarrow 170^\circ$  is largest interior angle
9.  $2x + \frac{1}{5}x + 3 = 47 \Rightarrow \frac{11}{5}x = 44 \Rightarrow x = 20 \Rightarrow$  base length is 7
10.  $2x + 3x = 7x - 13 \Rightarrow 2x = 13 \Rightarrow$  three interior angles are  $13^\circ$ ,  $19.5^\circ$ , and  $147.5^\circ$   
Smallest angle is  $13^\circ$
11. Angle intercepts  $200^\circ$  arc, so angle has measure  $\frac{1}{2}(200^\circ) = 100^\circ$
12. Man walks net of 125 feet north and 300 feet east. The hypotenuse has length 325.
13.  $\sqrt{9^2 + 6^2 + 3^2} = \sqrt{81 + 36 + 9} = \sqrt{126} = 3\sqrt{14}$
14.  $\sqrt{9^2 + 40^2} = \sqrt{81 + 1600} = \sqrt{1681} = 41$
15. Distance from center of hole to center of sphere is  $\sqrt{10^2 - 8^2} = \sqrt{100 - 64} = \sqrt{36} = 6$ ,  
so farthest distance is from center to far side of sphere through the center.

$$6+10=16$$

16. Circle has equation  $x^2 + (y-2)^2 = 6 \Rightarrow a=0, b=2, r=\sqrt{6} \Rightarrow a+b+r=2+\sqrt{6}$

17.  $\frac{\frac{4}{3}\pi r^3}{(2r)^3} = \frac{\frac{4}{3}\pi r^3}{8r^3} = \frac{\pi}{6}$

18.  $\frac{d}{C} = \frac{2r}{2\pi r} = \frac{1}{\pi}$

19. ratio of areas is  $\frac{2k^2}{18k^2} = \frac{1}{9}$ , so the ratio of the perimeters is  $\frac{1}{3}$

20.  $\frac{1}{2}(8+5)h=26 \Rightarrow h=4$

21.  $V = \frac{1}{3} \cdot 6 \left( \frac{4^2\sqrt{3}}{4} + \frac{6^2\sqrt{3}}{4} + \sqrt{\left(\frac{4^2\sqrt{3}}{4}\right)\left(\frac{6^2\sqrt{3}}{4}\right)} \right) = 2(4\sqrt{3} + 9\sqrt{3} + 6\sqrt{3}) = 38\sqrt{3}$

22.  $8^2 + (R-2)^2 = (R+2)^2 \Rightarrow 64 + R^2 - 4R + 4 = R^2 + 4R + 4 \Rightarrow 64 = 8R \Rightarrow R=8 \Rightarrow A = \pi \cdot 8^2 = 64\pi$

23.  $\pi r^2 \cdot 8 = 320\pi \Rightarrow r^2 = 40 \Rightarrow r = 2\sqrt{10}$

24. ratio of smaller triangle area to larger triangle area is  $\left(\frac{1}{2}\right)^2 = \frac{1}{4}$ , so the ratio of the smaller triangle's area to the area of the trapezoid is  $\frac{1}{4-1} = \frac{1}{3}$

25. triangle is right, so  $15h = 12 \cdot 9 \Rightarrow h = 108/15 = 36/5$