

For all questions, answer choice "E) NOTA" means none of the above answers is correct.

1. Solve for x : $21 \leq 3x + 11$

- A) $x \geq \frac{10}{3}$ B) $x \leq \frac{10}{3}$ C) $x \geq -\frac{10}{3}$ D) $x \leq -\frac{10}{3}$ E) NOTA

2. Find the value of $\frac{A}{B}$ if A and B are real numbers satisfying $4A + 6Bi = (3 + 2i)(1 - 3i)$.

- A) $\frac{9}{4}$ B) $-\frac{7}{6}$ C) $-\frac{27}{14}$ D) $-\frac{9}{7}$ E) NOTA

3. Solve for x : $\begin{vmatrix} 1 & 3 & 2 \\ 4 & x & 6 \\ 5 & 2 & 1 \end{vmatrix} = 0$

- A) 12 B) $\frac{82}{9}$ C) $\frac{64}{9}$ D) 16 E) NOTA

4. Solve for x : $2(2(x+3) - (x+1) \cdot 3) = 18$

- A) 4 B) -6 C) 6 D) 8 E) NOTA

5. A triangle has side lengths A , B , and C . If $A = 8$ and $B = 11$, then C must satisfy which inequality?

- A) $3 < C < 19$ B) $4 \leq C \leq 18$ C) $6 < C < 12$ D) $8 < C < 16$ E) NOTA

6. Find the sum of the solutions to the equation $x^3 = 27$.

- A) 0 B) 3 C) 9 D) -3 E) NOTA

7. The roots of the polynomial $f(x) = x^4 - 2x^3 - 53x^2 + 54x + 504$ are a_1 , a_2 , a_3 , and a_4 .

Find the value of $a_1a_2 + a_1a_3 + a_1a_4 + a_2a_3 + a_2a_4 + a_3a_4$.

- A) 54 B) -54 C) 53 D) -53 E) NOTA

8. Solve for x : $4^{3x+4} = 32^{x-1}$

- A) 0 B) 9 C) 17 D) -13 E) NOTA

9. How many integer solutions does the inequality $|6x - 4| \leq 14$ have?

- A) 4 B) 5 C) 8 D) 10 E) NOTA

10. Find the area of the region defined by the inequality $\frac{481}{144} - \frac{10}{9}x + \frac{1}{9}x^2 - \frac{3}{8}y + \frac{1}{16}y^2 \leq 1$.

- A) 9π B) 12π C) 16π D) 18π E) NOTA

11. If $f(3-x) = \frac{x^2 - 6x}{x+2}$, which of the following is equivalent to $f(x+1)$?

- A) $\frac{x^2 + 2x - 8}{-x + 6}$ B) $\frac{x^2 - 6x}{x + 6}$ C) $\frac{x^2 + 2x - 8}{-x + 2}$ D) $\frac{x^2 + 2x}{-x + 5}$ E) NOTA

12. If $f(x) = 2^x + 11$, find the domain of $f^{-1}(x)$.

- A) $x \geq 11$ B) $x > 11$ C) $x > 2$ D) all real numbers E) NOTA

13. Evaluate: $\sqrt{90 + \sqrt{90 + \sqrt{90 + \dots}}}$

- A) $\frac{1 + \sqrt{129}}{2}$ B) $13\frac{1}{2}$ C) 10 D) -9 E) NOTA

14. If $f(x) = 6x + \frac{11}{x} - 3$ and $g(x) = x^2$, find the value of $g(f(2))$.

- A) $841\frac{1}{2}$ B) $841\frac{1}{4}$ C) $2\frac{1}{211}$ D) $871\frac{1}{8}$ E) NOTA

15. Given the equation $\frac{\sqrt{24 - 8\sqrt{5}}}{\sqrt{6 + 2\sqrt{5}}} = a + b\sqrt{c}$, where a , b , and c are integers such that c is not divisible by the square of any prime number, find the value of the product abc .

- A) -15 B) -30 C) 15 D) 30 E) NOTA

16. Solve for x : $x^2 + 5x - 8 \geq 2x^2 + 2$

- A) $x > 6$ B) $x > 1$ C) $x > -5$ D) $x > -2$ E) NOTA

17. Find the zeros of the function $f(z) = 15z^2 + 16z + 4$.

- A) $-\frac{1}{3}, -\frac{9}{5}$ B) $-5, -\frac{1}{3}$ C) $-2, -1$ D) $-\frac{2}{3}, -\frac{2}{5}$ E) NOTA

18. Find the value of $A+B+C$, where A , B , and C are real numbers such that

$$\frac{21x^2 + 166x + 321}{(x+3)(x+4)(x+5)} = \frac{A}{x+3} + \frac{B}{x+4} + \frac{C}{x+5}.$$

- A) 19 B) 23 C) 21 D) 25 E) NOTA

19. Find the value of x in the solution to the system $\begin{cases} 2x + y = 16 \\ y + 6z = 5 \\ x + 3z = 4 \end{cases}$.

- A) -6 B) 2 C) 4.75 D) 6 E) NOTA

20. Solve for x : $(x+3)(x-4) > (x-6)(x+2)$

- A) $x > 0$ B) $x < 0$ C) $x > 4$ D) $x < 4$ E) NOTA

21. Find the area of the region defined by the inequality $2|x| + 3|y| \leq 1$.

- A) 6 B) $\frac{1}{3}$ C) $\frac{4}{3}$ D) $\frac{2}{3}$ E) NOTA

22. Given that $x+2y=1$, $y+2z=2$, and $z+2x=6$, find the value of $x+y+z$.

- A) 1 B) 12 C) 9 D) 3 E) NOTA

23. If A and B are the solutions to the equation $2 = 8 + \frac{5}{x} + \frac{1}{x^2}$, find the value of $\frac{1}{A} + \frac{1}{B}$.

- A) -5 B) 5 C) $\frac{5}{6}$ D) $-\frac{5}{6}$ E) NOTA

24. What is the largest coefficient in the expansion of $(3x+5y)^4$?

- A) 625 B) 1350 C) 1500 D) 1800 E) NOTA

25. Given the system of equations
$$\begin{cases} 2x + y + 2z = 4 \\ x + 2y + 3z = -1 \\ 3x + 2y + z = 9 \end{cases}$$
, find the value of $x + y + z$.

- A) -1 B) 3.5 C) 2 D) 1 E) NOTA

26. Find the sum of the coefficients in the expansion of $(x+1)^7$.

- A) 94 B) 117 C) 128 D) 256 E) NOTA

27. Find the sum of the real solutions to the equation $(x^2 - x - 1)^{x^2 - x - 6} = 1$.

- A) 5 B) 1 C) 2 D) 3 E) NOTA

28. Given that $\frac{1}{2}$ and $-\frac{1}{2}$ are two of the solutions to the equation $2x^3 + Ax^2 + Bx - \frac{3}{2} = 0$, where A and B are real numbers, find the value of $A + B$.

- A) 6 B) $\frac{11}{2}$ C) $\frac{13}{2}$ D) 0 E) NOTA

29. Given the function
$$f(x) = \begin{cases} 2x, & \text{if } 0 \leq x < 5 \\ -x, & \text{if } 5 \leq x < 10 \\ x^2, & \text{if } x < 0 \\ 1, & \text{if } x \geq 10 \end{cases}$$
, find the value of $f(f(f(f(f(f(f(2)))))))$.

- A) 8 B) 1 C) 2 D) -8 E) NOTA

30. Find the sum of the real solutions to the equation $|4x - |3x + 2|| = 6$.

- A) $\frac{48}{7}$ B) $\frac{24}{7}$ C) $\frac{20}{7}$ D) $\frac{52}{7}$ E) NOTA