

REMEMBER-----NOTA means None of the Above.

1. The sequence $\{r^n\}$ converges if and only if

- a) $|r| < 1$ b) $|r| \leq 1$ c) $-1 < r \leq 1$
 d) $0 < r < 1$ e) NOTA

2. If $\frac{1}{n(n+1)} = \frac{1}{n} - \frac{1}{n+1}$ ($n \geq 1$), then $\sum_{n=1}^{\infty} \frac{1}{n(n+1)} =$

- a) $\frac{4}{3}$ b) 1 c) $\frac{3}{2}$ d) $\frac{3}{4}$ e) NOTA

3. For which of the following series does the Ratio Test fail?

- a) $\sum \frac{1}{n!}$ b) $\sum \frac{n}{2^n}$ c) $\sum \frac{n^n}{n!}$
 d) $1 + \frac{1}{2^{3/2}} + \frac{1}{3^{3/2}} + \frac{1}{4^{3/2}} + \dots$ e) NOTA

4. $\sum_{n=1}^{\infty} \left(\frac{2}{3}\right)^n =$

- a) 1 b) $\frac{3}{2}$ c) $\frac{4}{3}$ d) 2 e) NOTA

5. The series $\sum_{n=0}^{\infty} n!(x-3)^n$ converges if and only if

- a) $x = 0$ b) $2 < x < 4$ c) $x = 3$ d) $2 \leq x \leq 4$
 e) NOTA

6. The coefficient of $\left(x - \frac{\pi}{4}\right)^3$ in the Taylor Series about $\frac{\pi}{4}$ of $f(x) = \cos x$ is

- a) $\frac{\sqrt{3}}{12}$ b) $\frac{-1}{12}$ c) $\frac{1}{12}$ d) $\frac{\sqrt{2}}{12}$ e) NOTA

7. If $e^{-0.1}$ is computed using series, then, correct to 3 decimal places, it equals

- a) 0.905 b) 0.903 c) 0.904 d) 0.900
 e) NOTA

8. The coefficient of $(x-1)^5$ in the Taylor series for $x \ln x$ about $x=1$ is

- a) $\frac{-1}{20}$ b) $\frac{1}{5!}$ c) $\frac{-1}{5!}$ d) $\frac{1}{20}$ e) NOTA

9. The radius of convergence of the series

$$\sum_{n=1}^{\infty} \frac{x^n}{2^n} \cdot \frac{n^n}{n!} \text{ is}$$

- a) 0 b) 2 c) $\frac{2}{e}$ d) $\frac{e}{2}$ e) NOTA

10. The sum of the series $\sum_{n=1}^{\infty} \left(\frac{\pi^3}{3^\pi}\right)^n$ is

- a) 0 b) 1 c) $\frac{3^\pi}{\pi^3 - 3^\pi}$ d) $\frac{\pi^3}{3^\pi - \pi^3}$
e) NOTA

11. When $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{3n-1}$ is approximated by the sum of its first 300 terms, the error is closest to

- a) 0.001 b) 0.002 c) 0.003
d) 0.004 e) NOTA

12. The series

$$(x-1) - \frac{(x-1)^2}{2!} + \frac{(x-1)^3}{3!} - \frac{(x-1)^4}{4!} + \dots \text{ converges}$$

- a) only for $0 < x < 2$ b) only for $0 \leq x < 2$
c) only for $0 < x \leq 2$ d) only if $x = 1$ e) NOTA

13. The coefficient of x^3 in the Maclaurin Series (about $x = 0$) of $\ln(1-x)$ is

- a) $-\frac{2}{3}$ b) $-\frac{1}{2}$ c) $-\frac{1}{3}$ d) $-\frac{1}{4}$ e) NOTA

14. $\lim_{n \rightarrow \infty} \frac{1 + \sqrt{2} + \sqrt{3} + \dots + \sqrt{n}}{n^{3/2}}$ is equal to the definite integral

- a) $\int_0^1 \sqrt{x} dx$ b) $\int_0^1 \frac{1}{\sqrt{x}} dx$ c) $\int_1^2 \sqrt{x} dx$
d) $\int_0^1 \frac{1}{x} dx$ e) NOTA

15. By differentiating term by term the series $(x-1) - \frac{(x-1)^2}{4} + \frac{(x-1)^3}{9} - \frac{(x-1)^4}{16} + \dots$ the interval of convergence obtained is

- a) $0 \leq x \leq 2$ b) $0 \leq x < 2$ c) $0 < x \leq 2$
d) $0 < x < 2$ e) NOTA

16. Find the limit of the sequence $\left\{ \frac{-9 + (-1)^n}{n!} \right\}$

- a) -9 b) 0 c) 1
d) The sequence diverges e) NOTA

17. Determine which of the following converge.

20. Determine the error when the sum of the series $\sum_{n=0}^{\infty} \frac{2}{5^n}$ is approximated by its 1st 3 terms.

a) $\sum_{n=1}^{\infty} \frac{1}{n}$ b) $\sum_{n=0}^{\infty} 3\left(\frac{4}{3}\right)^n$ c) $\sum_{n=1}^{\infty} \frac{1}{n^{0.3}}$

a) 0.02 b) 0.2 c) 0.01 d) 0.1 e) NOTA

d) $\sum_{n=1}^{\infty} \frac{1}{n^{3/2}}$ e) NOTA

21. Determine how many terms are needed for the error to the sum of the series in the above problem (#20) to be less than 0.0002.

a) 3 b) 4 c) 5 d) 6 e) NOTA

18. Determine which series diverges.

a) $\sum_{n=0}^{\infty} \frac{1}{2^n}$ b) $\sum_{n=0}^{\infty} (4 + (-1)^n)$

c) $\sum_{n=0}^{\infty} \left(\frac{1}{n} - \frac{1}{n+1}\right)$ d) $\sum_{n=1}^{\infty} \frac{1}{n^2}$ e) NOTA

22. Find the sum of the following series:

$$\frac{1}{\sqrt{2}+1} + \frac{1}{\sqrt{3}+\sqrt{2}} + \frac{1}{\sqrt{4}+\sqrt{3}} + \dots + \frac{1}{\sqrt{25}+\sqrt{24}}$$

a) 1 b) 2 c) 3 d) 4 e) NOTA

19. Which test could be used to show that

$$\sum_{n=1}^{\infty} \frac{n}{8n^3 + 6n^2 - 7} \text{ converges?}$$

23. Choose an equivalent series with the index of summation beginning at $n = 0$ for $\sum_{n=2}^{\infty} \frac{n2^n}{n-1}$.

- a) Geometric Series Test b) p-Series Test
c) Integral Test d) Limit Comparison Test
e) NOTA

a) $\sum_{n=0}^{\infty} \frac{n2^n}{n-1}$ b) $\sum_{n=0}^{\infty} \frac{(n-2)2^{n-2}}{n-3}$
c) $\sum_{n=0}^{\infty} \frac{(n+2)2^{n+2}}{n+1}$ d) $\sum_{n=0}^{\infty} \frac{(n+1)2^{n+1}}{n}$ e) NOTA

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24. The n th term of a sequence is signified by t_n .
For all $n > 1$, $t_1 + t_2 + t_3 + \dots + t_n = n^2 t_n$ and $t_1 = \frac{1}{2}$.

Find the exact value of $t_1 + t_2 + t_3 + \dots + t_{50}$.

- a) $\frac{49}{50}$ b) $\frac{50}{51}$ c) $\frac{51}{52}$ d) $\frac{52}{53}$ e) NOTA

25. Find the exact numerical value of

$$1 + 3\left(\frac{1}{3}\right) + 5\left(\frac{1}{3}\right)^2 + 7\left(\frac{1}{3}\right)^3 + 9\left(\frac{1}{3}\right)^4 + \dots$$

- a) e b) 3 c) π d) 5 e) NOTA

26. Evaluate: $\sum_{k=1}^{n+1} (2k-1) - \sum_{k=1}^n (2k-1)$

- a) $2n$ b) $2n + 1$ c) $2n - 1$ d) n e) NOTA

27. Evaluate: $\sum_{i=1}^{\infty} \frac{i}{5^i}$

- a) $\frac{1}{4}$ b) $\frac{5}{16}$ c) $\frac{1}{2}$ d) $\frac{3}{4}$ e) NOTA

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28. Find the sum of the first 100 terms of the
sequence: $\frac{2}{1 \cdot 3}, \frac{2}{3 \cdot 5}, \frac{2}{5 \cdot 7}, \dots, \frac{2}{(2n-1)(2n+1)}$

- a) $\frac{198}{199}$ b) $\frac{199}{200}$ c) $\frac{200}{201}$ d) $\frac{201}{202}$ e) NOTA

29. Find the sum of the 1st 22 terms of the
geometric progression having a 1st term of i , and
ratio of $(1+i)$, where $i = \sqrt{-1}$. Answer in the
form $c + di$, where c and d are real numbers.

- a) $1 + 2048i$ b) $1 - 2048i$ c) $-1 + 2048i$
d) $-1 - 2048i$ e) NOTA

30. If $x_n^2 - x_{n-1}x_{n+1} = (-2)^n$ for $n \geq 1$, and
 $x_0 = x_1 = 1$, then $x_3 = ?$

- a) 1 b) -3 c) 3 d) 5 e) NOTA