

For all questions, answer E "NOTA" means none of the above answers is correct.

1. Evaluate: $\int_9^{16} \frac{1}{\sqrt{x-4}} dx$

- A. $4\sqrt{3} - 2\sqrt{5}$ B. $4\sqrt{5} - 2\sqrt{3}$ C. $2\sqrt{3} - 4\sqrt{5}$ D. $4\sqrt{3} - 5\sqrt{2}$ E. NOTA

2. Find the *average value* of $f(x) = 2 + x - x^{-2}$ over the interval $1 \leq x \leq 3$.

- A. $11/3$ B. $22/3$ C. $11/6$ D. $10/3$ E. NOTA

3. Evaluate: $\int_0^5 |2 - x| dx$

- A. $-5/2$ B. $5/2$ C. $11/2$ D. $13/2$ E. NOTA

4. Use the Trapezoidal rule with $n = 4$ to approximate $\int_0^4 \sqrt{x^2 + 1} dx$.

- A. $(1 + \sqrt{2} + \sqrt{5} + \sqrt{10} + \sqrt{17}) / 2$ B. $1 + \sqrt{2} + \sqrt{5} + \sqrt{10} + \sqrt{17}$
 C. $(1 + 2\sqrt{2} + 2\sqrt{5} + 2\sqrt{10} + \sqrt{17}) / 2$ D. $1 + 2\sqrt{2} + 2\sqrt{5} + 2\sqrt{10} + \sqrt{17}$ E. NOTA

5. Evaluate: $\int_1^9 e^{\sqrt{x}} dx$

- A. e^3 B. $2e^3$ C. $3e^3$ D. $4e^3$ E. NOTA

6. A region R is bounded by the graphs $y = e^x$, $x = 0$, $x = e$, and $y = 0$. Find the volume of the solid generated when R is revolved about the y-axis.

- A. $2\pi[e^{e+1} + e^e + 1]$ B. $2\pi[e^{e+1} - e + 1]$ C. $2\pi[e^{e+1} - e^e - 1]$
 D. $2\pi[e^{e+1} - e^e - 2]$ E. NOTA

7. Evaluate $\int (e^\pi / x - \ln x + e^{-\pi}) dx$ on the interval $(1, e^\pi)$.

- A. $e^\pi - 1$ B. $2\sinh \pi$ C. $e^\pi + 1$ D. $2\cosh \pi$ E. NOTA

8. Given $y = \int_2^x \cos(\pi^3 t) dt$, find the equation of the tangent line at $x = 2$.

- A. $x + y = 2$ B. $x + y = 3$ C. $x - y = 2$ D. $2x - y = 3$ E. NOTA

9. Evaluate: $\int_{\pi/2}^{3\pi/4} \sin^2(2t) dt$

- A. $\pi/2$ B. $\pi/4$ C. $\pi/6$ D. $\pi/8$ E. NOTA

10. Evaluate: $\int \frac{\log_{10}(x^4 10^x)}{x} dx$

- A. $\frac{(\ln x)^2}{2 \ln 10} + x + C$ B. $\frac{2(\ln x)^2}{\ln 10} + x + C$ C. $\frac{4(\ln x)^2}{\ln 10} + x + C$
 D. $\frac{(\ln x)^2}{4 \ln 10} + x + C$ E. NOTA

11. Evaluate: $\int_0^2 \frac{1}{(2x-1)^{2/3}} dx$

- A. $3\sqrt[3]{2} / 2$ B. $3(1-\sqrt[3]{3}) / 2$ C. $2\sqrt[3]{2} / 3$ D. $3(1+\sqrt[3]{3}) / 2$ E. NOTA

12. Find the particular solution of $\frac{du}{dt} = \frac{t+3t^2}{u^2}$, given $u = 6$ when $t = 0$. So u equals

- A. $\sqrt[3]{t^2/2+3t^3+72}$ B. $\sqrt[3]{3t^2/2+3t^3+72}$ C. $\sqrt[3]{3t^2/2+3t^3+216}$
 D. $\sqrt[3]{t^2/2+3t^3+216}$ E. NOTA

13. What is the coefficient of the x^{13} term of $\int \left[\frac{x^3}{2} - 2 \right]^8 dx$?

- A. 56/17 B. 60/13 C. 70/13 D. 80/17 E. NOTA

14. Which of the following is equal to $\int \cos x \csc x dx$?

- A. $\ln|\cos x| + C$ B. $\ln|\sin x| + C$ C. $-\ln|\cos x| + C$ D. $-\ln|\sec x| + C$ E. NOTA

15. Find the area A of the region that lies within the limaçon $r = 1 + 2\cos\theta$ and outside the circle $r = 2$.

- A. $\frac{15\sqrt{3}-\pi}{6}$ B. $\frac{12\sqrt{3}-2\pi}{6}$ C. $\frac{9\sqrt{3}-2\pi}{6}$ D. $\frac{15\sqrt{3}-2\pi}{6}$ E. NOTA

16. Evaluate: $\int_1^3 \frac{x+1}{x^2+2x+3} dx$

- A. $2 \ln \sqrt{3}$ B. $\ln \sqrt{3}$ C. $2 \ln 3$ D. $\ln 3$ E. NOTA

17. A particle starts at rest and moves along the x-axis, its acceleration given by $a(t) = t + \cos(2t)$ for $t \geq 0$. If the particle is located at $x = 0$ when $t = 0$, which x-value is the particle located when $t = \pi$?

- A. $\pi^3 + \frac{1}{4}$ B. $\pi^3/6 + \frac{1}{2}$ C. $\pi^3/6$ D. $\pi^3/2 + \frac{1}{4}$ E. NOTA

18. Evaluate: $\int_0^1 \int_0^{\pi/2} (e^y + \sin x) dx dy$

- A. $\frac{\pi(e-1)}{2} + 1$ B. $\pi(e+1)$ C. $\frac{\pi(e+1)}{2}$ D. $\frac{\pi(e-1)}{2} - 1$ E. NOTA

19. What is the area of the region bounded between the graphs of $y = x + 1$ and $y = 3 - x^2$?

- A. $5/3$ B. $7/3$ C. $9/2$ D. $11/2$ E. NOTA

20. If $g(x) = \int_1^{2x^2} (t-4) dt$, over what interval(s) is the graph of $y = g(x)$ concave up?

- A. $(-\infty, -\sqrt{2}) \cup (\sqrt{2}, \infty)$ B. $(-\infty, -\sqrt{2/3}) \cup (\sqrt{2/3}, \infty)$ C. $(-\sqrt{2/3}, \sqrt{2/3})$
 D. $(-\sqrt{2}, \sqrt{2})$ E. NOTA

21. Evaluate the limit: $\lim_{x \rightarrow 1} \frac{\int_1^x 2(t \ln t - t + e^{t-1} + \pi) dt}{x^2 - 1}$

- A. $\pi/2$ B. π C. $3\pi/2$ D. 2π E. NOTA

22. Find $\int \frac{x}{(2x+d)^2} dx$, where $d \in \mathbb{Z}^+$ (d is a positive integer).

- A. $\frac{1}{4} \ln |2x+d| + \frac{d}{4(2x+d)} + C$ B. $\frac{1}{4} \ln |2x+d| - \frac{d}{4(2x+d)} + C$ C. $\frac{1}{4} \ln |2x-d| + \frac{d}{4(2x-d)} + C$
 D. $\frac{1}{2} \ln |2x+d| + \frac{d}{2(2x+d)} + C$ E. NOTA

23. A particle moves along the line with velocity $v(t) = 4t^3$ (ft/sec). Find the *total distance* traveled (in feet) between time $t = -2$ and time $t = 3$.

- A. 64 B. 65 C. 95 D. 97 E. NOTA

24. Suppose $f(x) = \ln(\pi x)$ and $f^{-1}(x)$ is its inverse. Then $\int f^{-1}(x)dx$ equals

- A. $\frac{e^x}{\pi} + C$ B. $\frac{\pi}{e^x} + C$ C. $e^{\pi x} + C$ D. $e^x + \pi$ E. NOTA

25. The area bounded by the curve $y = x^2$ and the line $y = 4$ is divided into two equal portions by the line $y = c$. Find the value of c .

- A. $2\sqrt{2}$ B. $\sqrt[3]{9}$ C. $\sqrt[3]{16}$ D. $\frac{3\sqrt{3}}{2}$ E. NOTA

26. The base of a solid is the region bounded by $y = 1 - x^2$ and $y = 1 - x^4$. Cross-sections of the solid that are perpendicular to the x -axis are squares. The expression to find the *volume* of the solid is

- A. $\int_{-1}^1 (x^4 - x^2)^2 dx$ B. $2 \int_0^1 (x^2 - x^4)^2 dx$ C. $2 \int_{-1}^1 (x^2 - x^4)^2 dx$
 D. $2 \int_0^1 [(1 - x^4)^2 - (1 - x^2)^2] dx$ E. NOTA

27. Evaluate: $\int \sin^3 x \cos^{-4} x dx$

- A. $(\sec^3 x)/3 + \sec x + C$ B. $(\csc^3 x)/3 - \csc x + C$ C. $\sec x - (\sec^3 x)/3 + C$
 D. $(\sec^3 x)/3 - \sec x + C$ E. NOTA

28. Find the area of the surface generated by revolving the curve with parametric equations $x = t$, $y = t^3$ on the interval $0 \leq t \leq 1$ about the x -axis .

- A. $\pi(10\sqrt{10} - 1)/9$ B. $\pi(10\sqrt{10} + 1)/9$ C. $\pi(\sqrt{10} - 1)/27$ D. $\pi(10\sqrt{10} + 1)/27$ E. NOTA

29. Evaluate: $\int_{-100}^{100} (v + \sin v + v \cos v + \sin^3 v)^5 dv$

- A. 0 B. 50 C. 100 D. 200 E. NOTA

30. Determine the value of $\int_0^{1/2} \frac{1}{1-x^2} dx$.

- A. $\ln 2$ B. $\ln \sqrt{2}$ C. $\ln \sqrt{3}$ D. $\ln \sqrt{5}$ E. NOTA