

For all questions, answer choice "E) NOTA" means none of the above answers is correct.

1. Find the equation of the line perpendicular to $3x - 2y = 5$ containing the point $(-2, 3)$.

- A) $3x - 2y = -12$ B) $2x - 3y = -19$ C) $2x + 3y = 5$ D) $3x + 2y = 0$ E) NOTA

2. Find the area of $\triangle ABC$ with vertices $A(-1, 4)$, $B(2, 5)$, and $C(4, -3)$.

- A) 31 B) 21 C) 18 D) 13 E) NOTA

3. For $f(x) = ax^2 - bx + c$, if $f(2) = 3$ and $x = -3$ is a zero of the function, find $a + b$.

- A) $-\frac{3}{5}$ B) $\frac{3}{2}$ C) $-\frac{2}{3}$ D) $\frac{5}{3}$ E) NOTA

4. Find the x -value of the ordered pair of the intersection of $y = |x - 1| - 3$ and $y = 2x - 1$.

- A) $-\frac{2}{3}$ B) $-\frac{1}{3}$ C) $\frac{1}{3}$ D) $\frac{2}{3}$ E) NOTA

5. Given $f(x) = x^2 - x - 1$ and $g(x) = 2f(x) - 3f(x - 1)$, find $g(3) - f(1)$.

- A) 31 B) 27 C) 28 D) 6 E) NOTA

6. Let $A =$ the sum of the solutions to the equation $9(3^{x^2 - 2x}) = 3^{4 - x}$, and let $B =$ the sum of the solutions to the equation $2^{3y - 1} = 4^{y^2}$. Find the value of the product AB .

- A) -1 B) $-\frac{2}{3}$ C) $\frac{3}{2}$ D) 2 E) NOTA

7. If $\sqrt{3 + \sqrt{3 + \sqrt{3 + \dots}}} - \sqrt{2 + \sqrt{2 + \sqrt{2 + \dots}}}$ can be written in the form $\frac{a + \sqrt{b}}{c}$, where a , b , and c are relatively prime integers and b is not divisible by the square of any integer, find the value of $a + b - c$.

- A) 1 B) 5 C) 8 D) 16 E) NOTA

8. If three fair dimes are tossed, what are the odds that 2 heads and 1 tail are shown?

- A) 5:3 B) 3:5 C) 3:8 D) 5:8 E) NOTA

9. Which of the following is the inverse of $f(x) = \frac{x-1}{x+2}$?

- A) $f^{-1}(x) = \frac{x+2}{x-1}$ B) $f^{-1}(x) = \frac{x-2}{x+1}$ C) $f^{-1}(x) = \frac{2x+1}{1-x}$ D) $f^{-1}(x) = \frac{2x-1}{x-1}$ E) NOTA

10. What is the minimum value of the function $f(x) = 2x^2 - 5x - 8$?

- A) -8 B) -10.375 C) -11.125 D) -12 E) NOTA

11. Solve the equation $\log_a 3 - \log_a b = c$ for b .

- A) $b = \frac{c}{3a}$ B) $b = \frac{3}{a^c}$ C) $b = \frac{a}{3c}$ D) $b = a^{3c}$ E) NOTA

12. The following table gives some values of $f(x)$ and $f^{-1}(x)$. What is the value of $a + b$?

| | | | | | | | |
|-------------|---|---|---|-----|---|---|---|
| x | 0 | 1 | 2 | 3 | 4 | 5 | ? |
| $f(x)$ | 5 | 3 | ? | a | ? | 4 | 8 |
| $f^{-1}(x)$ | 2 | 4 | 3 | b | ? | ? | 8 |

- A) 3 B) 4 C) 5 D) 6 E) NOTA

13. How many distinct permutations of the letters A , B , C , and D exist?

- A) 6 B) 12 C) 20 D) 24 E) NOTA

14. Find the value of the following: $\sum_{c=2}^7 \frac{1}{c+1} - \sum_{c=2}^7 \frac{1}{c-1}$

- A) $-\frac{23}{27}$ B) $-\frac{69}{56}$ C) $\frac{15}{56}$ D) $-\frac{61}{56}$ E) NOTA

15. The area of a rectangle remains unchanged when side A is made 2.5 units longer and side B is made $\frac{2}{3}$ units narrower OR when side A is made 2.5 units shorter and side B is made $\frac{4}{3}$ units wider. Find the area of the rectangle.

- A) 10 B) 20 C) 40 D) 50 E) NOTA

16. Joe is trying to solve a quadratic equation, but parts of the equation are missing. He knows that the sum of the roots is the same as that of the equation $2x^2 - 3x - 5 = 0$ and the product of the roots is the same as that of the equation $3x^2 + x - 3 = 0$. Which of the following is one solution to Joe's equation?

- A) 0.5 B) -2 C) -0.25 D) 2 E) NOTA

17. Find the value of $\sqrt[3]{27 - 54b + 36b^2 - 8b^3}$ if $b = 4$.

- A) -3 B) -2 C) 4 D) 5 E) NOTA

18. Suppose f is a quadratic function for which $f(0) = 4$, $f(1) = 5$, and $f(-1) = f(0) + f(1)$. Find the value of $f(5)$.

- A) 69 B) 89 C) 93 D) 98 E) NOTA

19. Let A = the radius of the circle with equation $9x^2 + 9y^2 - 54x + 36y = -101$, and let B = the length of the major axis of the ellipse with equation $25x^2 + 9y^2 + 100x - 90y = -100$, find the value of $3A - 2B$.

- A) -8 B) -16 C) -5 D) 1 E) NOTA

20. Find the number of lattice points in the region defined by $y > 0$, $x > 0$, $2x - y < 8$, and $4x + 5y < 30$.

- A) 17 B) 16 C) 15 D) 14 E) NOTA

21. If $z = x + yi$, then $z\bar{z} + (-3 + 4i)\bar{z} + (-3 - 4i)z = 0$ is the equation of a circle, where \bar{z} is the complex conjugate of z . Find the coordinates of the center of the circle.

- A) (4, -3) B) (-3, 4) C) (3, -4) D) (4, 3) E) NOTA

22. Which of the following is the domain of the inverse of the function $f(x) = 3x^2 - 4x - 3$, $x \geq 3$?

- A) $[12, \infty)$ B) $(-\infty, \infty)$ C) $(-\infty, 3]$ D) $[-\frac{13}{3}, \infty)$ E) NOTA

23. Given that $\frac{3i}{i+3} - \frac{i}{i-3} = a - bi$, where a and b are real numbers, find the value of $a + b$.

- A) -1 B) $\frac{7}{5}$ C) $\frac{7}{10}$ D) 1 E) NOTA

24. The solution to the equation $\log_8(x+1) - \log_8(x-1) = \frac{2}{3}$ can be written in the form $\frac{a}{b}$, where a and b are relatively prime positive integers. Find the value of a^b .

- A) 8 B) 243 C) 125 D) 256 E) NOTA

25. Find the product AB^{-1} if $A = \begin{bmatrix} -1 & 3 \\ 2 & 5 \\ 0 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & 5 \\ -2 & -4 \end{bmatrix}$.

- A) $\begin{bmatrix} 10 & 1 \\ 2 & 20 \\ 8 & -8 \end{bmatrix}$ B) $\begin{bmatrix} 8.5 & 7 \\ 10.5 & 8 \\ -10 & -6 \end{bmatrix}$ C) $\begin{bmatrix} -1 & 0.5 \\ -9 & 10 \\ 4 & -4 \end{bmatrix}$ D) $\begin{bmatrix} 5 & 5.5 \\ 1 & 0 \\ -4 & -4 \end{bmatrix}$ E) NOTA

26. Find the solutions set of the inequality $\frac{x-2}{x-3} \leq 2$.

- A) $(-\infty, 3] \cup [4, \infty)$ B) $(3, 4]$ C) $(-\infty, 3) \cup (4, \infty)$ D) $[4, \infty)$ E) NOTA

27. Circles O and P intersect at points G and H . The radii of O and P have lengths of 5 and 6, respectively, and $|\overline{OP}| = 7$. Find the length of \overline{GH} .

- A) $\frac{12\sqrt{6}}{7}$ B) $\frac{8\sqrt{3}}{7}$ C) $\frac{12\sqrt{42}}{7}$ D) $\frac{24\sqrt{6}}{7}$ E) NOTA

28. Find the largest value of x for which $\begin{vmatrix} -2 & 4 & 0 \\ 3 & x & 3 \\ -1 & 1 & 5 \end{vmatrix} = 7x^2 - 74$

- A) 2 B) $-\frac{4}{7}$ C) $\frac{4}{7}$ D) -2 E) NOTA

29. The degree measure of the smaller acute angle of a right triangle is equal to the sum of the squares of the roots of $x^2 - 7x + 5 = 0$. Find the degree measure of the larger acute angle.

- A) 69° B) 64° C) 57° D) 51° E) NOTA

30. Find the value of k such that the parabolas $y = 3x^2 + 16x + k$ and $y = -2x^2 - 4x + 6$ intersect in exactly one point.

- A) 26 B) 24 C) 6 D) -12 E) NOTA