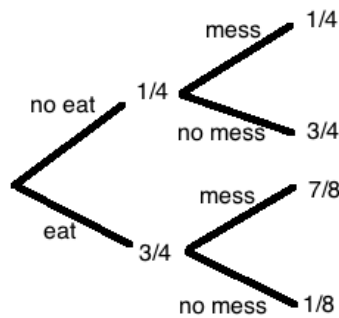


- B.** Each time the derivative is taken, the first term is multiplied by its exponent and the exponent has 1 subtracted from it, giving $(21!)x$. Using the Chain Rule on the second piece gives $(2)^{20}e^{2x}$. The first time the derivative is taken of $\ln x$, it results in $\frac{1}{x}$. Then the Power Rule is used repeatedly, causing the exponent in the denominator to increase each time, the signs in front to alternate, and the coefficients to multiply, to $(-1)^{19} \frac{18!}{x^{19}}$.
- A.** Rationalize the numerator: $\lim_{x \rightarrow 7} \frac{x+2-9}{(x-7)\sqrt{x+2}+3}$. The factors of $x-7$ cancel: $\lim_{x \rightarrow 7} \frac{1}{\sqrt{x+2}+3} = \frac{1}{6}$.
- D.** Divide through by 3 to get $x^2 + y^2 - 8x + 6y = 75$. Use implicit differentiation: $2x + 2y \left(\frac{dy}{dx}\right) - 8 + 6 \left(\frac{dy}{dx}\right) = 0$, and solve for $\left(\frac{dy}{dx}\right)$ to get $\frac{dy}{dx} = \frac{4-x}{y+3}$. When $x = 10$, $y = 5$ or $y = -11$. Plugging in $(10, 5)$, $\frac{dy}{dx} = \frac{4-10}{5+3} = -\frac{3}{4}$. Plugging in $(10, -11)$, $\frac{dy}{dx} = \frac{4-10}{-11+3} = \frac{3}{4}$. Their sum is 0.
- B.** The derivative is $h'(x) = -a \sin x + b \sec^2 x + c \sec x \tan x - d \csc^2 x + e \cos x - f \csc x \cot x$. Plugging in $\frac{\pi}{4}$: $a \left(\frac{\sqrt{2}}{2}\right) + b(2) + c(\sqrt{2}) - d(2) + e \left(\frac{\sqrt{2}}{2}\right) - f(\sqrt{2})$. Group the like terms together: $(e-a) \left(\frac{\sqrt{2}}{2}\right) + (b-d)(2) + (c-f)(\sqrt{2})$, then substitute in the given information: $(4) \left(\frac{\sqrt{2}}{2}\right) + (-3)(2) + (2)(\sqrt{2}) = 4\sqrt{2} - 6$.
- D.** Plug in 2 for x in each part, set equal: $16a + 10 = 4b - 6$. Take the derivative of each part, plug in 2 for x, set equal: $32a + 5 = 4b - 3$. Solve using elimination: $b = 6$.
- B.** Use u-substitution, with $u = \ln x$ and $du = \frac{1}{x} dx$. $\int u du = \frac{1}{2}u^2 = \frac{1}{2}(\ln x)^2 \Big|_1^e = \frac{1}{2}((\ln e)^2 - (\ln 1)^2) = \frac{1}{2}(1-0) = \frac{1}{2}$.
- D.** Find the zeros of the polynomial: $x = 1, x = 5$. The value of the polynomial is negative on the interval $(1, 5)$, so integrate both pieces separately. $\int_0^1 3x^2 - 18x + 15 dx - \int_1^5 3x^2 - 18x + 15 dx = x^3 - 9x^2 + 15x \Big|_0^1 - (x^3 - 9x^2 + 15x) \Big|_1^5 = (1 - 9 + 15 - 0) - [(125 - 225 + 75) - (1 - 9 + 15)] = 7 - (-32) = 39$.



- C.** Create a tree diagram:
 The formula for conditional probability is $P(A|B) = \frac{P(A \cap B)}{P(B)}$. Let A be that Mrs. Funk had to clean up a mess, and B be that the dog ate something bad for her. $P(A \cap B) = \left(\frac{3}{4}\right) \left(\frac{7}{8}\right) = \frac{21}{32}$. $P(B) = \left(\frac{3}{4}\right) \left(\frac{7}{8}\right) + \left(\frac{1}{4}\right) \left(\frac{1}{4}\right) = \frac{21}{32} + \frac{1}{16} = \frac{23}{32}$. Therefore, $P(A|B) = \frac{\frac{21}{32}}{\frac{23}{32}} = \frac{21}{23}$.
- A.** Use partial fraction decomposition: $\frac{A}{x} + \frac{B}{x-1} + \frac{C}{x+1} = \frac{x^2-2}{x^3-x} \rightarrow A(x^2-1) + B(x^2-x) + C(x^2+x) = x^2-2$. Set up equations with coefficients equal to each other: $A + B + C = 1$ from the x^2 terms, $-B + C = 0$ from the x

terms, $-A = -2$ from the constant terms: $A = 2$, $B = -\frac{1}{2}$, $C = -\frac{1}{2}$. Now integrate $\int \left(\frac{2}{x} - \frac{\frac{1}{2}}{x+1} - \frac{\frac{1}{2}}{x-1} \right) dx = 2 \ln x - \frac{1}{2} \ln(x+1) - \frac{1}{2} \ln(x-1) + C = \ln \frac{x^2}{\sqrt{x^2-1}} + C$.

10. **B.** The equation for horizontal distance traveled is $x(t) = 49t \cos(30^\circ)$ and for vertical distance is $y(t) = 49t \sin(30^\circ) - 4.9t^2$. First find the time when the cannonball hits the ground: $0 = 4.9t(10 \sin(30^\circ) - t) \rightarrow t = 10 \left(\frac{1}{2} \right) = 5$. Then plug in 5 for t in the horizontal distance: $x = 49(5) \left(\frac{\sqrt{3}}{2} \right) = \frac{245\sqrt{3}}{2}$.
11. **D.** Since we are concerned with the adjacent side and the hypotenuse, set up the equation $\cos \theta = \frac{7}{h}$. Use implicit differentiation: $-\sin \theta \left(\frac{d\theta}{dt} \right) = \frac{-7}{h^2} \left(\frac{dh}{dt} \right)$. If the hypotenuse is 25 inches, use Pythagorean theorem to find that the side opposite θ is 24 inches. Therefore, $\sin \theta = \frac{24}{25}$. Substitute into the equation: $\left(-\frac{24}{25} \right) \left(\frac{d\theta}{dt} \right) = \frac{-7}{25^2} (2) \rightarrow \frac{d\theta}{dt} = \frac{7}{300}$ radians per second.
12. **B.** Differentiate: $p'(t) = 30x^4 - 60x^2 - 90$. Set equal to zero and solve for x to find that the only real solutions are $x = \pm\sqrt{3}$. Their product is -3 . They must be maximums or minimums because neither of them satisfies the equation $p''(t) = 0$.
13. **B.** Newton's method states that $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$. $f'(x) = 3x^2 + 8x$. Therefore, $x_1 = -1 - \frac{1}{-5} = \frac{-4}{5}$ and $x_2 = -\frac{4}{5} - \frac{\frac{6}{125}}{\frac{-112}{25}} = -\frac{227}{280}$.
14. **E.** $f(x) = x^2 - x^3$ and $f'(x) = 2x - 3x^2$. Set the derivative equal to zero and solve for x : $x = \frac{2}{3}$ or $x = 0$. Since zero will not provide a maximum, $\frac{2}{3}$ is our answer.
15. **A.** Let x equal the width of the rectangle, which will be the radius of our cylinder. Since the perimeter must equal 12, the height is $6-x$. The volume of the cylinder is $V = \pi x^2(6-x)$. Differentiate to get $V' = \pi(12x - 3x^2) = 0 \rightarrow x = 4$. The dimensions to maximize the volume of the cylinder are 4 inches by 2 inches.
16. **A.** Use synthetic division to divide the polynomials: $\int \left(x^2 + 2x + 4 + \frac{8}{x-2} \right) dx = \frac{1}{3}x^3 + x^2 + 4x + 8 \ln|x-2| + C$.
17. **D.** Since $\int_{10}^3 f(x) dx = 7$, $\int_3^{10} f(x) dx = -7$. $\int_1^3 f(x) dx + \int_3^{10} f(x) dx = \int_1^{10} f(x) dx \rightarrow \int_1^3 f(x) dx - 7 = 4 \rightarrow \int_1^3 f(x) dx = 11$.
18. **B.** Find $f(5)$ and $f'(5)$: $f(5) = \sqrt{(5)^4 - 16(5)^2} = \sqrt{225} = 15$, $f'(x) = \frac{2x^3 - 16x}{\sqrt{x^4 - 16x^2}}$, $f'(5) = \frac{250 - 80}{(15)} = \frac{170}{15} = \frac{34}{3}$. Since we are finding the line normal to the graph, use the perpendicular slope. The line has slope $-\frac{3}{34}$ and passes through the point $(5, 15)$, therefore the line is $y - 15 = -\frac{3}{34}(x - 5)$.
19. **C.** Solve for y : $\pm y = \sqrt{x^2 - 9}$, and use only the positive portion since the graph is in the first quadrant only. To find the volume: $\pi \int_3^5 \left(\sqrt{x^2 - 9} \right)^2 dx = \pi \left(\frac{1}{3}x^3 - 9x \right) \Big|_3^5 = \pi \left(\frac{125}{3} - 9(5) - \left(\frac{27}{3} - 9(3) \right) \right) = \pi \left(-\frac{10}{3} - (-18) \right) = \frac{44\pi}{3}$.

20. **B.** $\frac{dy}{dt} = 1$, $\frac{dx}{dt} = 2x - 3$. Therefore $\frac{dy}{dx} = \frac{1}{2x - 3}$. To find the second derivative, use the chain rule: $\frac{d}{dt} \left(\frac{dy}{dx} \right) = \frac{dx}{dt}$.
- Therefore, $\frac{d^2y}{dx^2} = \frac{-2}{(2t - 3)^2}$. Evaluate at $t = 2$: $\frac{-2}{(2(2) - 3)^2} = -2$.
21. **B.** $f'(x) = \frac{1}{2} \cos\left(\frac{x}{2}\right)$. Set equal to 0 and solve for x : $\cos\left(\frac{x}{2}\right) = 0 \rightarrow \frac{x}{2} = \frac{\pi}{2}, \frac{3\pi}{2} \rightarrow x = \pi, 3\pi$. However, only π is on the specified interval, so the sum of all solutions is π .
22. **C.** First, note that the height and radius of the full tank are proportional to the height and radius of the partially full tank, so find an expression for the radius: $\frac{2}{6} = \frac{r}{h} \rightarrow r = \frac{h}{3}$. Then substitute into the volume formula for a cone: $V = \frac{1}{3}\pi r^2 h = \frac{1}{27}\pi h^3$. Differentiate: $\frac{dV}{dt} = \frac{1}{27}\pi(3)(h^2) \left(\frac{dh}{dt}\right)$, then substitute in the known values: $\frac{dV}{dt} = \frac{1}{9}\pi(2)^2(0.2) = \frac{4\pi}{45}$.
23. **D.** $\int_0^a \sin x \, dx = -\cos x|_0^a = -\cos a + \cos 0 = 1 + \frac{\sqrt{2}}{2}$. There are two angles that satisfy this equation, $\frac{3\pi}{4}$ and $\frac{5\pi}{4}$. The sum of these is 2π .
24. **D.** To convert Cartesian coordinates to polar coordinates, $r = \sqrt{x^2 + y^2} = \sqrt{(\sqrt{3})^2 + (-1)^2} = \pm 2$. If $r = 2$: $\tan^{-1} \frac{-1}{\sqrt{3}} = -\frac{\pi}{6}$. This angle is coterminal to $\frac{11\pi}{6}$. If $r = -2$, then the radius extends in the negative direction and rotates $-\frac{\pi}{6}$, providing $\theta = \frac{5\pi}{6}$. Therefore $(-2, \frac{11\pi}{6}, 3)$ is not a possible representation of the point.
25. **A.** If a plane is perpendicular to a vector, then the components of the vector become the coefficients on the variables in the plane equation. $8x + 2y + 3z = d$, plug in the x , y , and z -coordinates of the point to find d : $8(7) + 2(12) + 3(-5) = d \rightarrow d = 65$.
26. **B.** Find the eigenvalues of the matrix: $\begin{vmatrix} 3 - \lambda & 2 \\ 1 & 4 - \lambda \end{vmatrix} = 0$, $\lambda^2 - 7\lambda + 10 = 0$, $(\lambda - 5)(\lambda - 2) = 0$, $\lambda = 5, 2$. To find the eigenvectors: $\begin{bmatrix} 3 & 2 \\ 1 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \lambda \begin{bmatrix} x \\ y \end{bmatrix}$. Use $\lambda = 5$ to find the system of equations $3x + 2y = 5x$, $x + 4y = 5y$. Both equations reduce to $x = y$, so that any vector with x - and y -components being equal is an eigenvector of this matrix.
27. **A.** Let S =sum of the infinite series. List out the first several terms: $S = \frac{2}{9} + \frac{4}{27} + \frac{6}{81} + \frac{8}{243} \dots$. Multiply the series by $\frac{1}{3}$: $\frac{S}{3} = \frac{2}{27} + \frac{4}{81} + \frac{6}{243} + \frac{8}{729} \dots$. Then subtract the two sums to get $\frac{2S}{3} = \frac{2}{9} + \frac{2}{27} + \frac{2}{81} + \frac{2}{243} \dots$. This is an infinite geometric series with first term $\frac{2}{9}$ and common ratio $\frac{2}{3}$. $\frac{2S}{3} = \frac{\frac{2}{9}}{1 - \frac{2}{3}} = \frac{1}{3}$. Solve for S to find that $S = \frac{1}{2}$.
28. **C.** In an odd function, $B(-x) = -B(x)$. Therefore, $\frac{B(B(B(-3)))}{3B(1) - 2B(3) - B(5)} = \frac{B(B(-5))}{3(2) - 2(5) - (1)} = \frac{B(-1)}{6 - 10 - 1} = \frac{-2}{-5} = \frac{2}{5}$.
29. **B.** Separate the differential equation: $4y^3 \, dy = e^{2x} \, dx$. Integrate both sides to get $y^4 = \frac{1}{2}e^{2x} + C$. Since $y(0) = 1$, $(1)^4 = \frac{1}{2}e^0 + C \rightarrow C = \frac{1}{2}$.
30. **B.** Use the product rule: $f'(x) = \sin x(-\sin x) + \cos x(\cos x)$. This simplifies to $\cos 2x$. $\cos 2\left(\frac{\pi}{4}\right) = 0$.